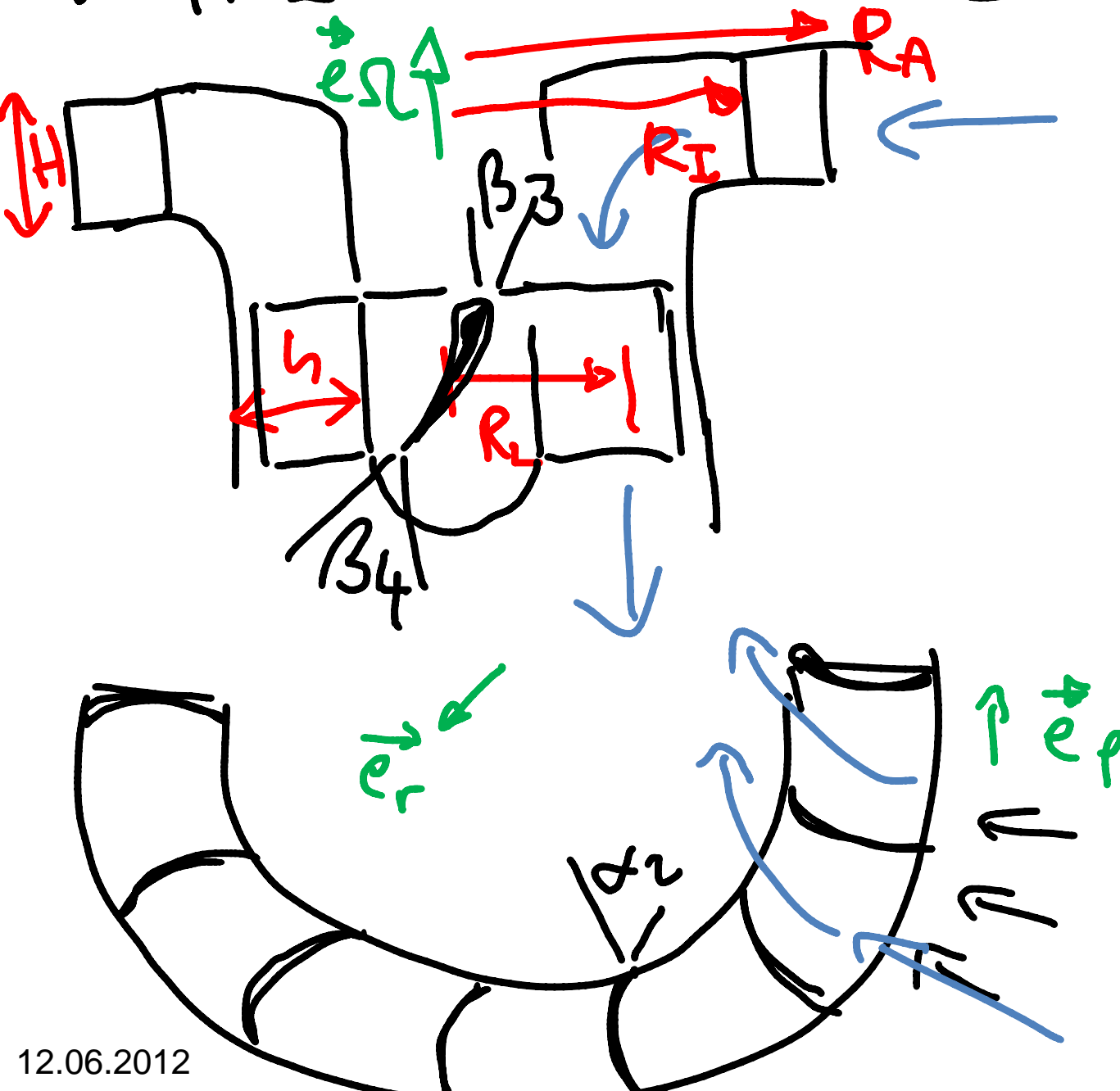


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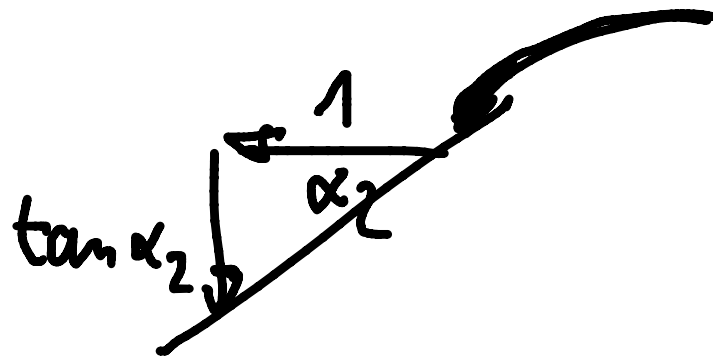
Einführung in die
Hydrodynamik
Vorrechenübung

Prof. Dr.-Ing. Peter Pelz
Sommersemester 2012
Übung 7 F 42



$$\vec{c}_1 = -\frac{Q}{2\pi R_a H} \vec{e}_r$$

$$\vec{c}_2 = -\frac{Q}{2\pi R_I H} \vec{e}_r + \frac{Q \tan \alpha_2}{2\pi R_I H} \vec{e}_\varphi$$



$$\tau_2 c_{u2} - \tau_3 c_{u3} = 0 \quad \text{Turbinengleichung}$$

Drallhaltung

$$\Rightarrow c_{u3} = \frac{Q \tan \alpha_2}{2\pi R_L H}$$

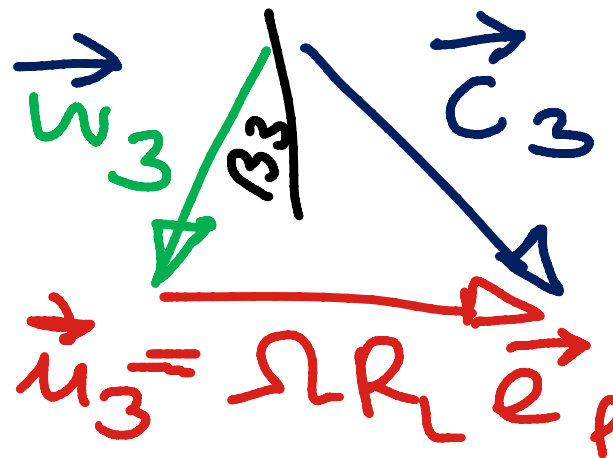
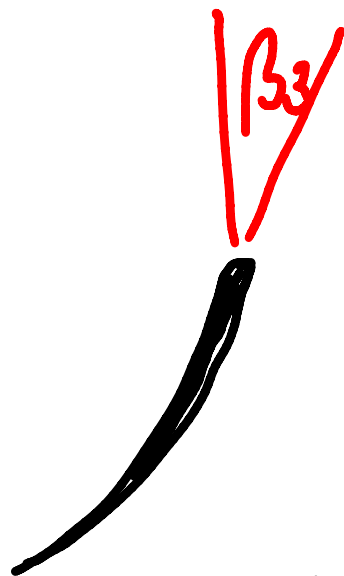


$$c_{3\Omega} = - \frac{Q}{2\pi R_L h}$$

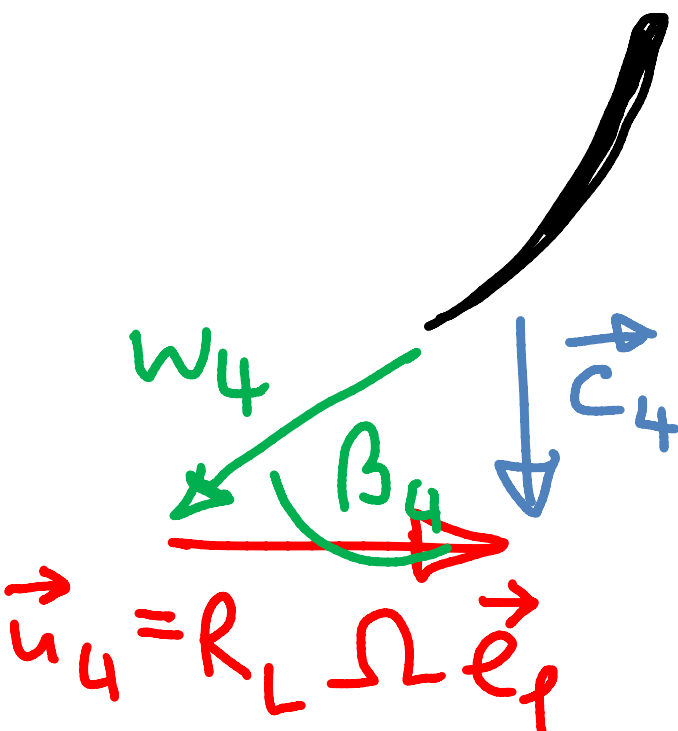
$$M = m(c_{m3} R_L - c_{m4} R_L)$$

$$M = \rho Q \frac{Q \tan \alpha_2}{2\pi R_L h} R_L = \rho \frac{Q^2 \tan \alpha_2}{2\pi h}$$

$$P_T = \vec{M} \cdot \vec{\Omega} = \rho \frac{Q^2 \Omega \tan \alpha_2}{2\pi h}$$



$$\begin{aligned} \tan \beta_3 &= \frac{w_{u3}}{|w_{\Omega 3}|} = \frac{\frac{Q \tan \alpha_2}{2\pi R_L h} - \Omega R_L}{\frac{Q}{2\pi R_L h}} \\ &= \frac{h}{H} \tan \alpha_2 - \frac{2\pi R_L^2 h \Omega}{Q} \end{aligned}$$



$$\tan \beta_4 = \frac{|w_4|}{|c_4|}$$
$$= \frac{\Omega R_L}{\frac{Q}{2\pi R_L h}}$$

$$\tan \beta_4 = \frac{2\pi R_L^2 h \Omega}{Q}$$