

Neutron-star mergers and the high-density equation of state

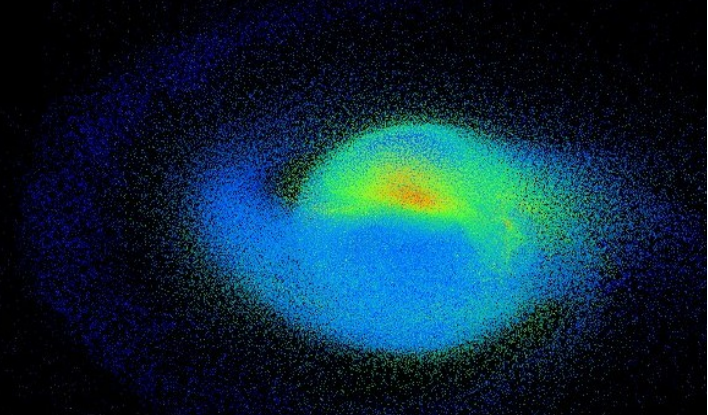
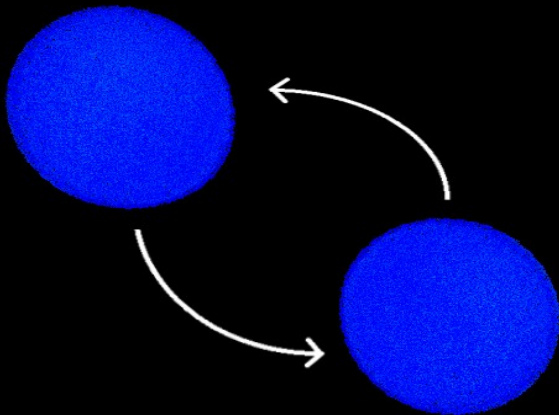
2nd workshop of the SFB 1245

Budenheim, 05/10/2017

Andreas Bauswein

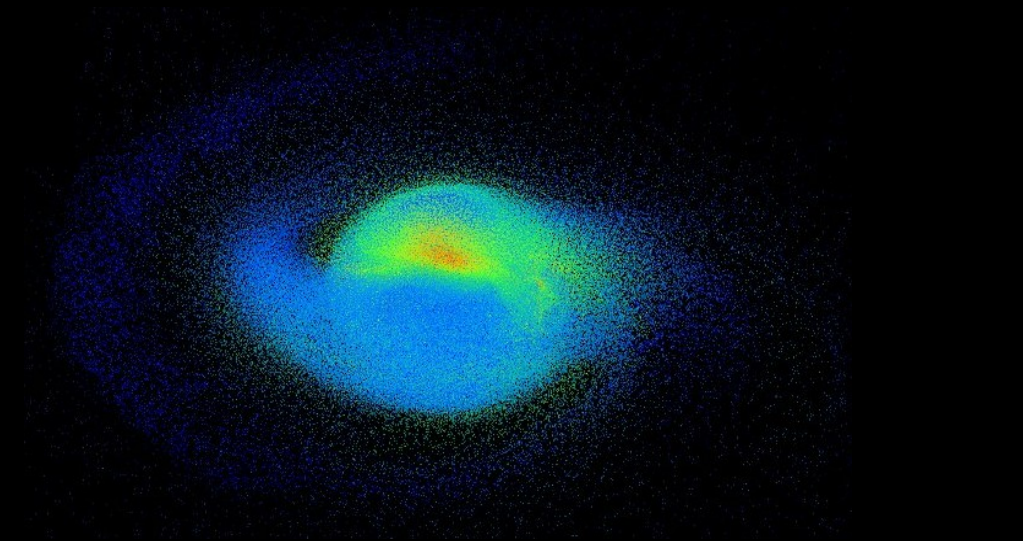
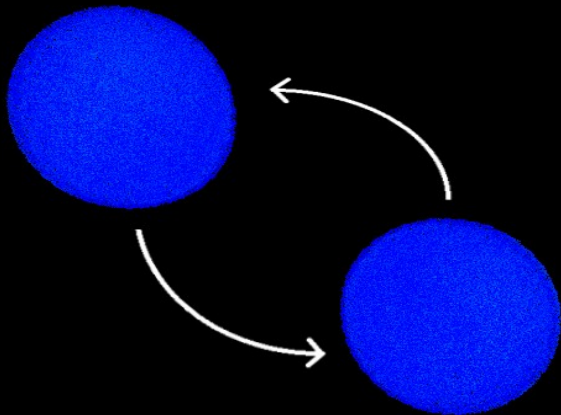
(Heidelberg Institute for Theoretical Studies)

with K. Chatziioannou, J. A. Clark, H.-T. Janka N. Stergioulas



Outline

- ▶ NS merger – motivation and overview
- ▶ Gravitational waves
- ▶ EoS constraints
 - dominant postmerger GW frequency → Radius measurement
 - collapse behavior → Maximum mass of NSs (very high density regime)
- ▶ GW data analysis
- ▶ Outlook: GW asteroseismology

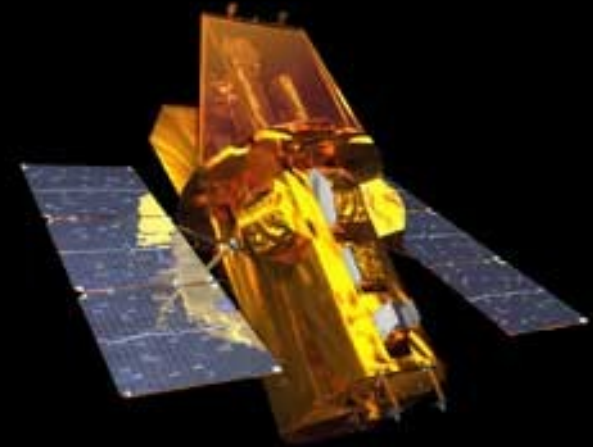


Overview - NS mergers

- ▶ Short gamma-ray bursts → high-energy astrophysics / gamma-ray astronomy
 - ▶ Site for the rapid neutron-capture process → heavy element formation
 - ▶ Electromagnetic transients → “time-domain astronomy”
 - ▶ **Gravitational wave emitters → EoS of nuclear matter**
-
- ▶ Btw: all these aspects are also related to NS-black hole mergers

Short gamma-ray bursts

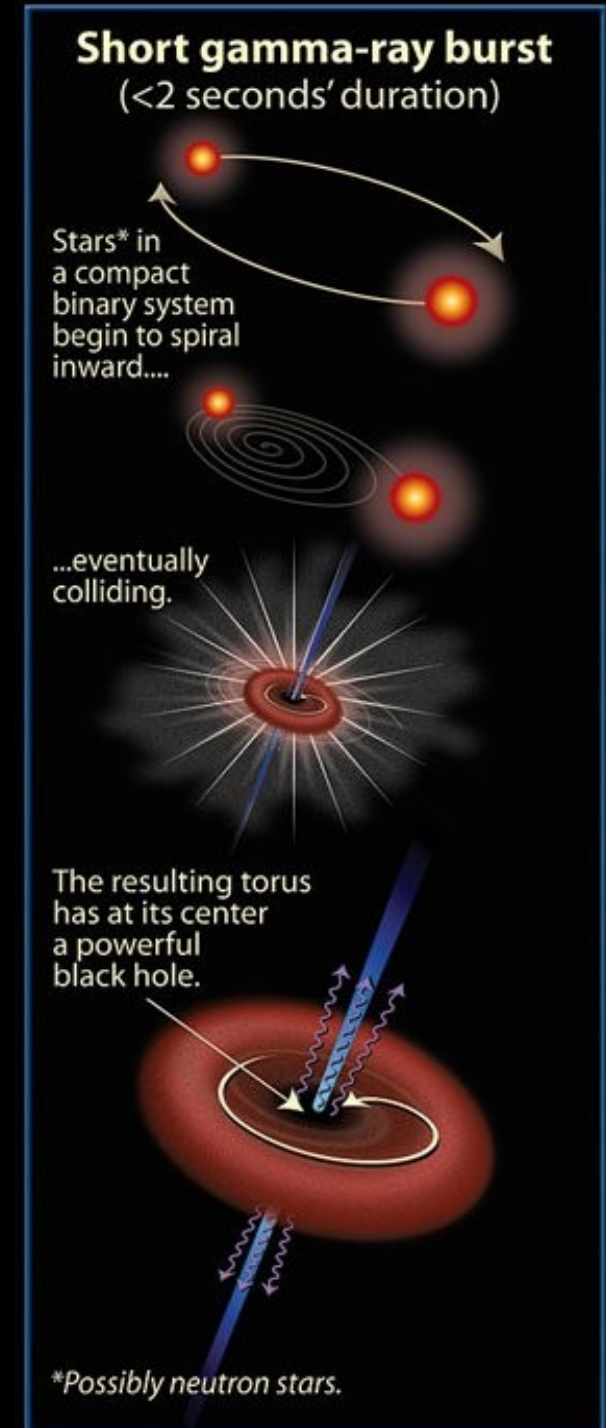
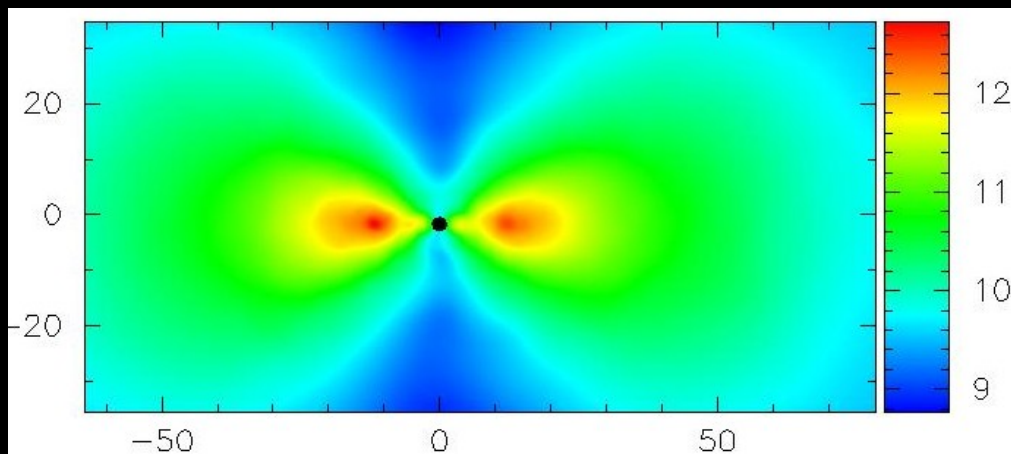
- ▶ Observed since the 70ies
- ▶ **Intense flashes of gamma rays** with duration $< \sim 2$ secs with $10^{50} \dots 10^{52}$ erg/s
- ▶ random, non-repeating, isotropic **at cosmological distances**
- ▶ (long GRBs with duration $> \sim 2$ secs produced by collapse of massive star – confirmed by supernova association = lightcurve observed; tend to be somewhat softer than short bursts)
- ▶ produced by jets (baryon-poor relativistic beamed outflow) forming from a BH-torus system after NS merger or NS-BH merger → **beamed emission**
- ▶ Afterglow (=interaction of jet with ambient medium) routinely observed as follow up with X-ray, optical, radio telescopes
- ▶ Some GRBs show X-ray plateau emission $\sim 100 \dots 1000$ seconds



Swift

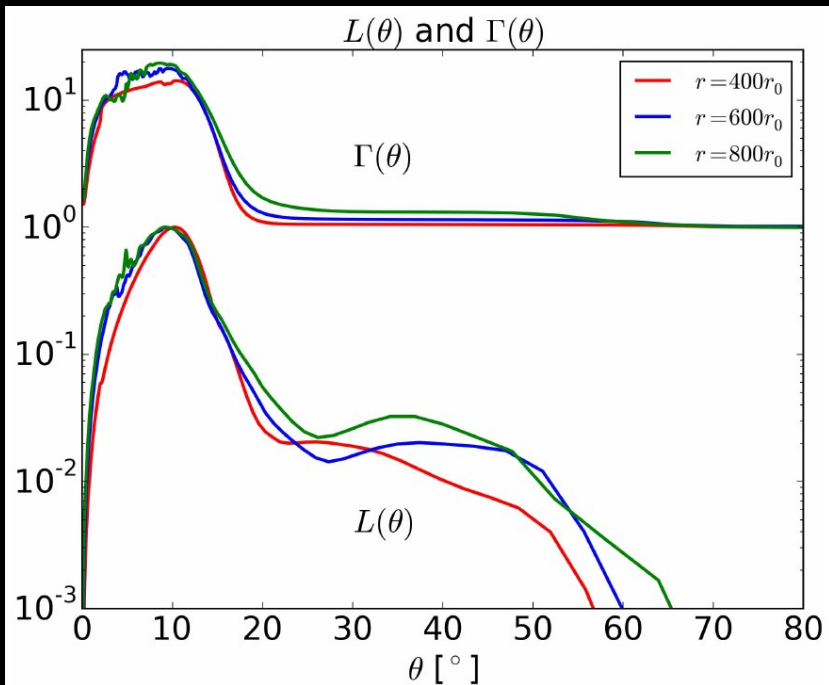
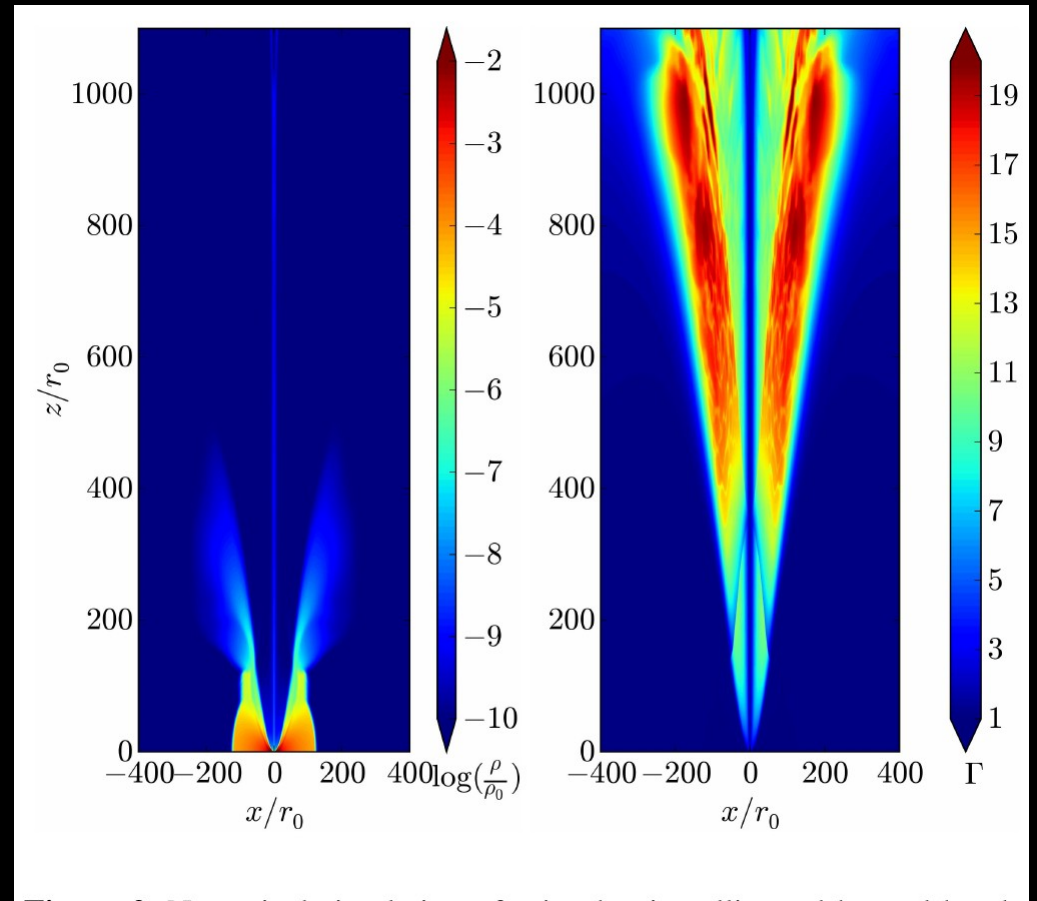
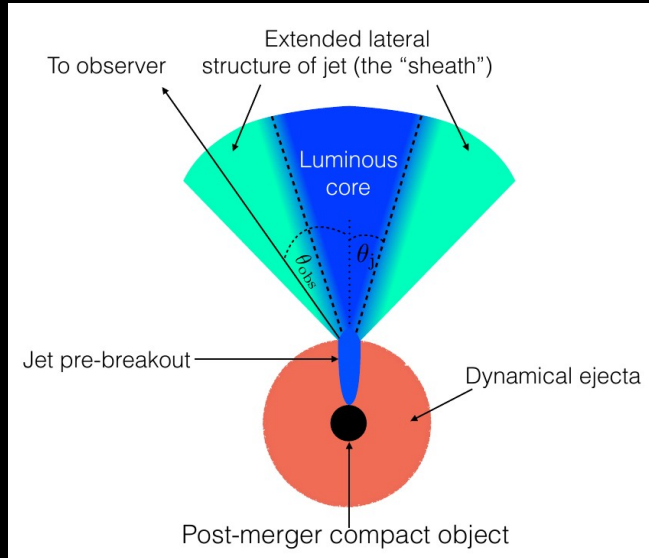
Short gamma-ray bursts

- ▶ Arguments for mergers as progenitors:
 - energetics and time scales
 - no supernova association (excluded with very good limits)
 - occurrence in star-forming and elliptical galaxies
 - off-center from host galaxies
 - rates (as far as we can estimate rates)
- ▶ Smoking gun: **coincident detection of sGRB and GWs**
 - estimate probability to see both simultaneously (assume opening angle ~ 10 deg.)



Off-axis emission

- ▶ May increase likelihood of coincident measurements



e.g. Kathirgamaraju et al. 2017

Nucleosynthesis

- ▶ Origin of heavy elements formed by **rapid-neutron capture process**
- ▶ Astrophysical production site of rapid neutron-capture elements not yet identified
 - **mergers provide favorable conditions**: ejecta neutron rich, fast expanding ejecta (typically $\sim 10^{-2} M_{\text{sun}}$)
 - many alternative scenarios, e.g. core-collapse supernovae
- ▶ R-process elements **observed in stellar spectra** of all metallicities especially metal-poor (=old) stars
 - points to certain robustness and universality of r-process
 - understand **galactic chemical evolution**
- ▶ Open questions
 - details of r-process path (ejecta properties, e.g. masses, temperatures, neutrinos, different types of ejecta: dynamical vs. secular, importance of fission)
 - nuclear physics models
 - overall production / dominant source ? → GW / em observations will settle rate
- ▶ Many groups involved from astro side and nuclear physics, e.g. in DA Arcones, Martinez-Pinedo, ...

Electromagnetic transients

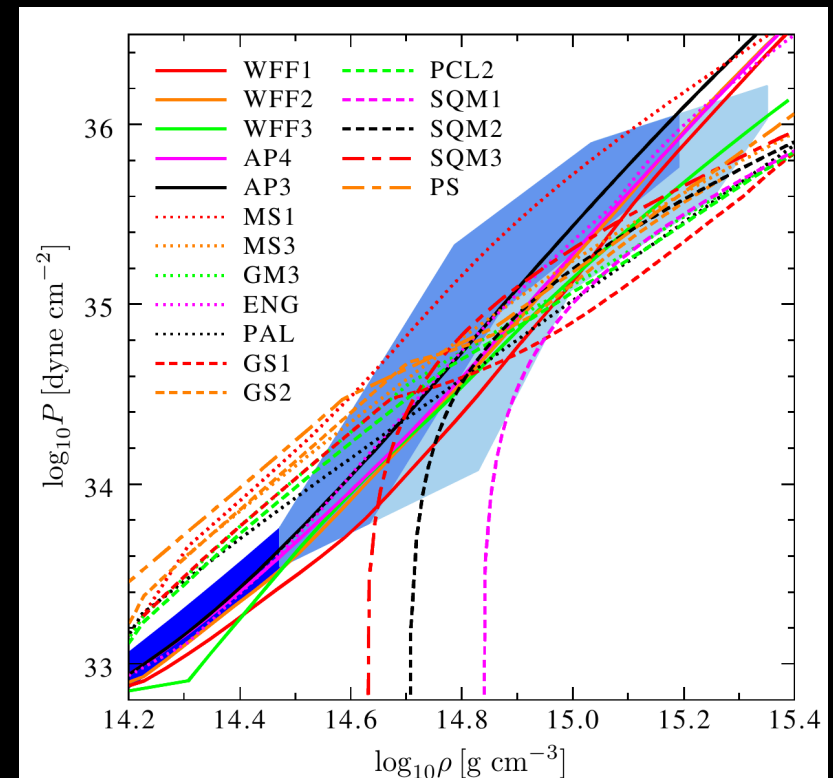
- ▶ Synonyms: “kilonova”, “macronova”
- ▶ Powered by radioactive decays during/after r-process → heat expanding ejecta
- ▶ Ejecta initially opaque → transparent on time scale of 1 d → peak luminosity
- ▶ Thermal emission in UV, optical, infrared
- ▶ Targets for time-domain astronomy
 - blind searched by surveys: Large Synoptic Survey Telescope (LSST), Palomar Transient Factory (PTF), BlackGEM, ...
 - triggered searches (by GW candidate, sGRB): Hubble Space Telescope, Very Large Telescope, ...
- ▶ Potential observations of radioactively powered transients in aftermath of sGRBs, e.g. GRB130603b

Electromagnetic transients - outlook

- ▶ **Electromagnetic counterpart to GW event** → increases confidence and sensitivity of GW searches by providing precise sky position
- ▶ Understand zoo of astronomical transient phenomena
- ▶ Rate of NS mergers
- ▶ Reveal details of nucleosynthesis: ejecta masses, velocities, abundances, ...
 - Rate * ejecta mass = total production
 - Is all gold produced in NS mergers?
- ▶ Particularly rewarding: **multi-messenger astronomy**
 - GW → binary masses, possibly EoS
 - em emission (sGRB / kilonova): sky position, dynamics of merger, ejecta masses

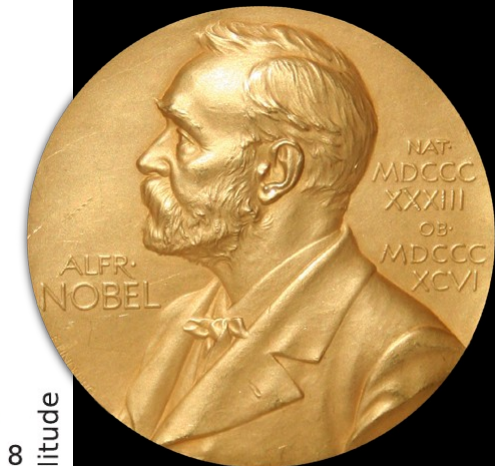
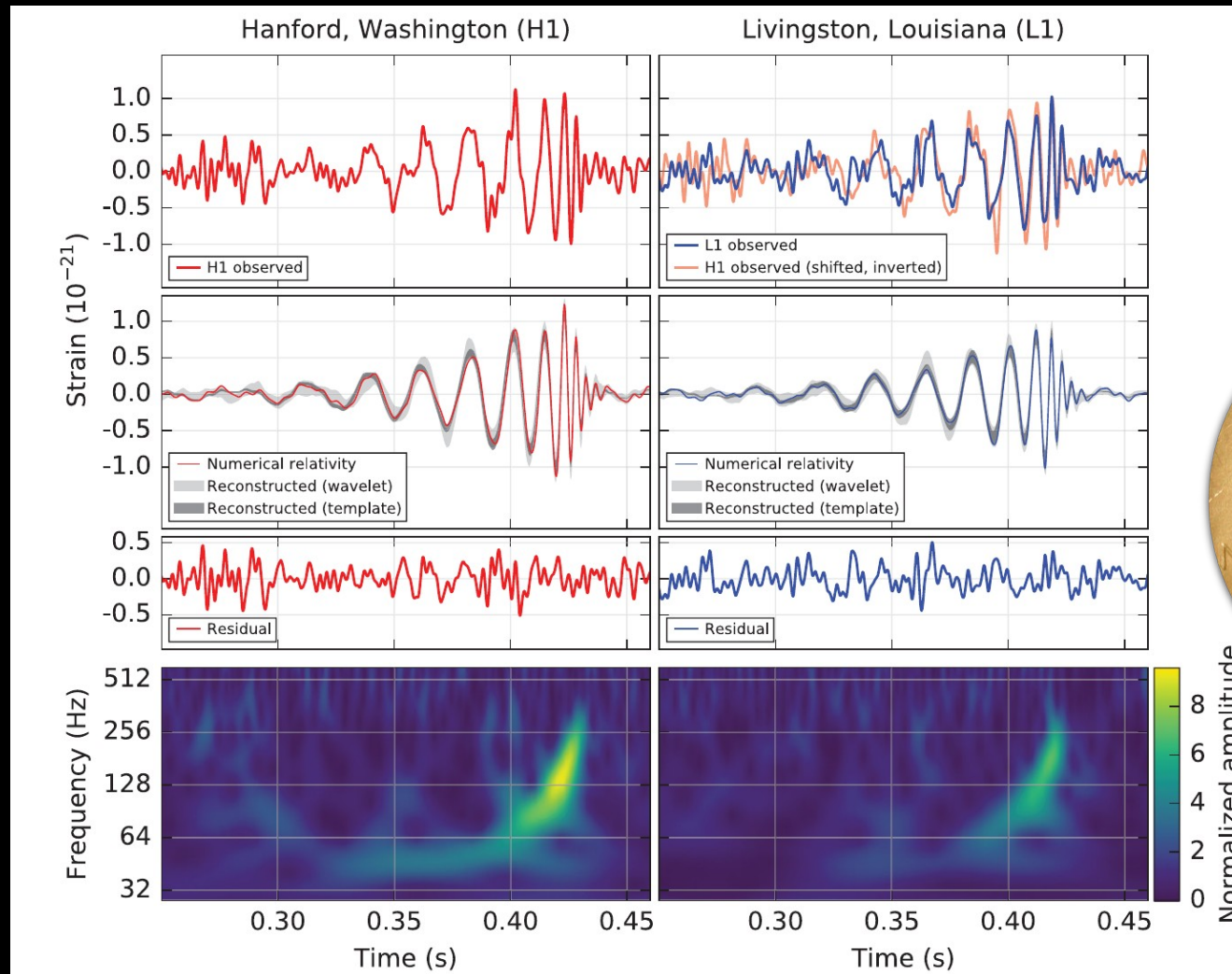
Gravitational waves

- ▶ NS mergers are **strong emitters of GWs** → next type of source to be detected
- ▶ Detections will clarify rate and binary masses of population
- ▶ GWs from NS mergers bear potential to **constrain EoS of high-density matter**
 - stiffness at saturation and beyond
 - hyperon puzzle
 - more exotic phases (QCD phase transition)
 -



Gravitational waves

GW150914: a BH-BH merger – first direct observation of GWs



2017

September 14, 2015

Abbott et al. 2016

Plus three more BH mergers

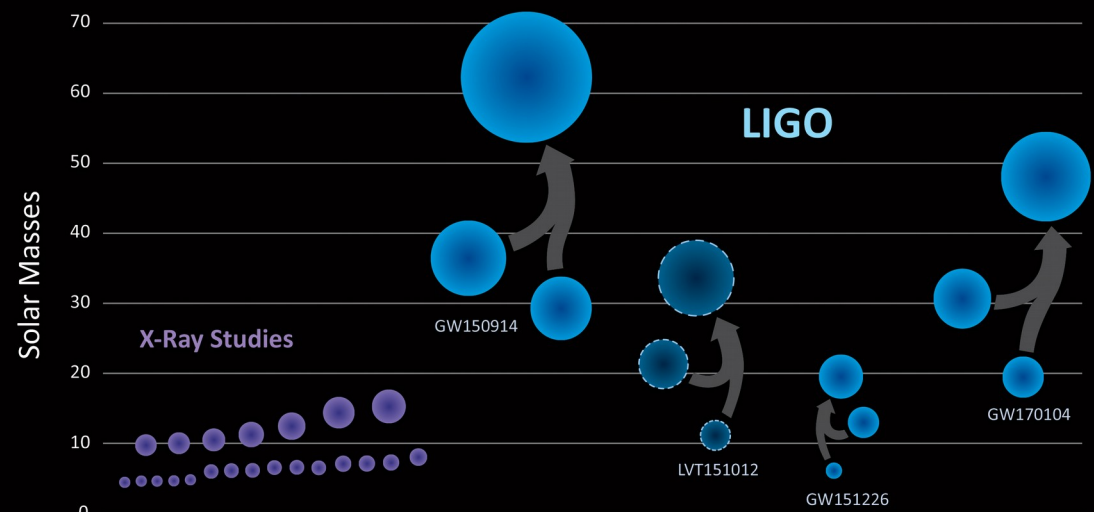
GWs from BH mergers

- ▶ First BH binaries detected
- ▶ GW signal reveals masses – orbital motion
 - any orbiting binary will produce a chirping signal → merger
- ▶ Rates
 - 4 BH mergers vs 0 NS mergers does not imply that rate of NS mergers is lower
 - NSM rate per volume is expected to be higher

Primary black hole mass m_1	$31.2^{+8.4}_{-6.0} M_{\odot}$ ←
Secondary black hole mass m_2	$19.4^{+5.3}_{-5.9} M_{\odot}$ ←
Chirp mass \mathcal{M}	$21.1^{+2.4}_{-2.7} M_{\odot}$
Total mass M	$50.7^{+5.9}_{-5.0} M_{\odot}$
Final black hole mass M_f	$48.7^{+5.7}_{-4.6} M_{\odot}$
Radiated energy E_{rad}	$2.0^{+0.6}_{-0.7} M_{\odot} c^2$
Peak luminosity ℓ_{peak}	$3.1^{+0.7}_{-1.3} \times 10^{56} \text{erg s}^{-1}$
Effective inspiral spin parameter χ_{eff}	$-0.12^{+0.21}_{-0.30}$
Final black hole spin a_f	$0.64^{+0.09}_{-0.20}$
Luminosity distance D_L	$880^{+450}_{-390} \text{Mpc}$
Source redshift z	$0.18^{+0.08}_{-0.07}$

GW170104 (Abbott et al. 2017)

Black Holes of Known Mass

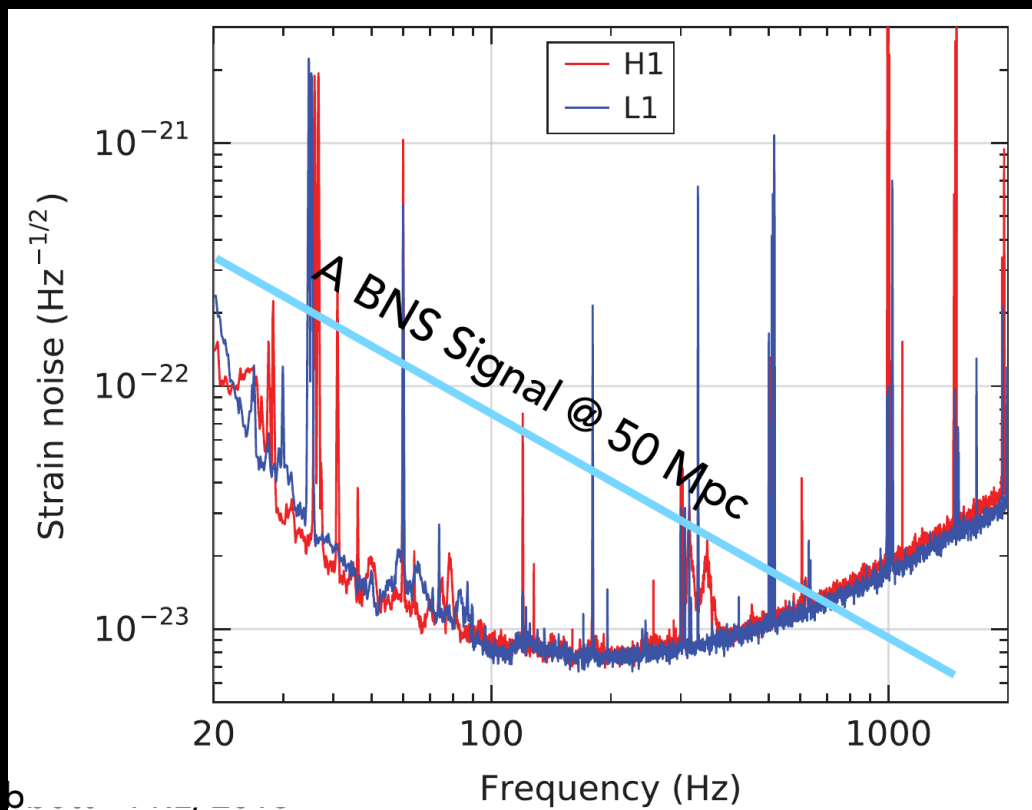


+ GW170814: 25+31 solar masses

Detector characteristics

- ▶ Fabry-Perot Michelson interferometer
- ▶ Different sources of noise: thermal, seismic, shot noise, ...
- ▶ Sensitive to GWs with frequencies between **a few 10 Hz to a few kHz**
 - frequency range determines types of observable sources (orbital/dynamical time scales)
 - stellar compact objects: NS stellar mass BHs
- ▶ Design sensitivity within next years (a few factors higher), more instruments become operational
- ▶ **Challenge: GW data analysis**, e.g.,
 - matched filtering: template based → requires complete model of expected signals
 - unmodelled searches
 - some proper statistical argument that some pattern was not a random fluctuation

Sensitivity (noise) curve of Adv. LIGO detectors during first observing run (O1) in 2016



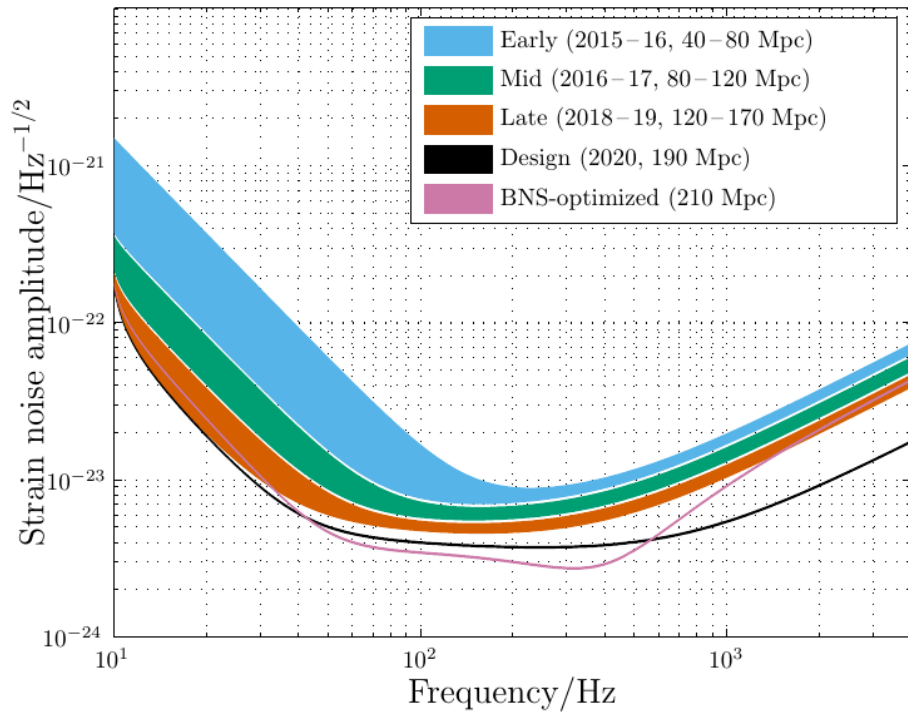
Seismic noise

Thermal noise

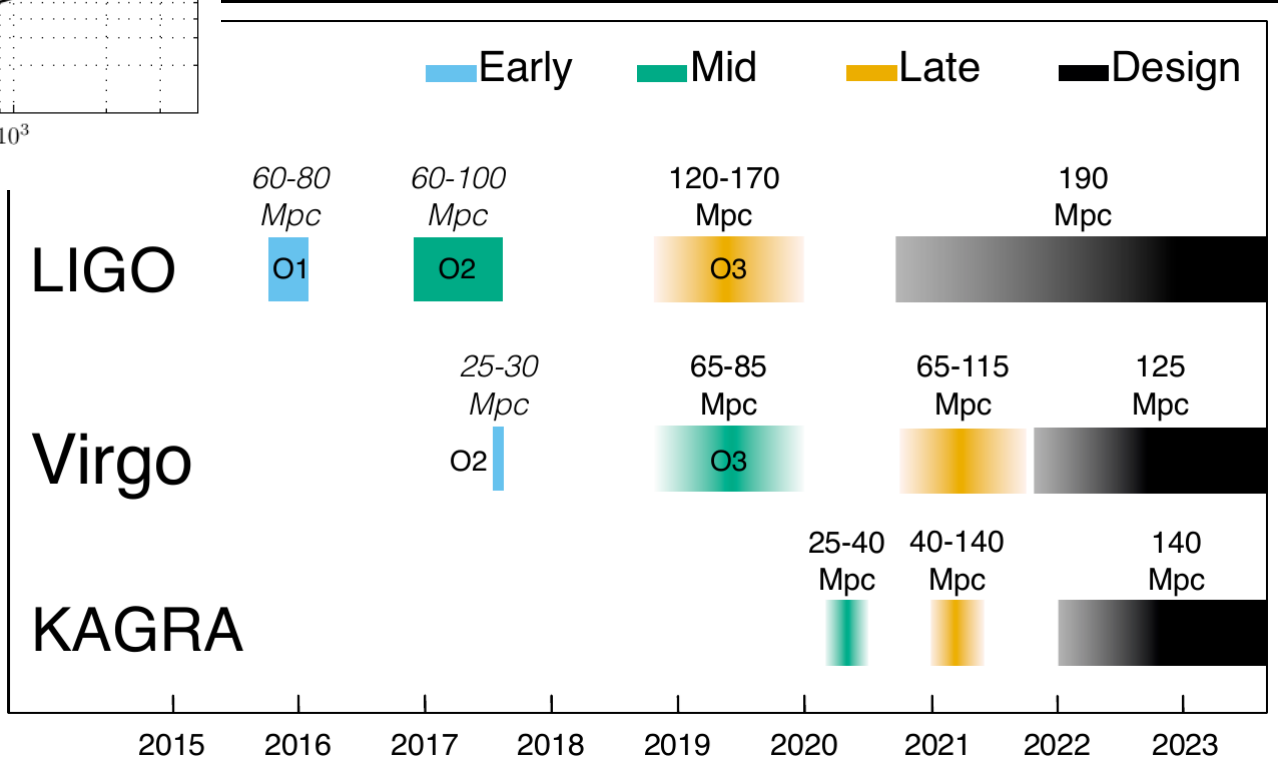
Photon shot

Future plans

Advanced LIGO



Abbott et al. 2017



Future

- ▶ More detectors become operational with higher sensitivity → network leads to higher overall sensitivity
- ▶ Plans for 3rd generation instruments and upgrades of current detectors:
 - Einstein Telescope
 - Voyager
 - Cosmic Explorer
 - LIGO +

(all similar frequency band: 10 Hz to several kHz, but different sensitivity)

- ▶ Laser Interferometer Space Antenna (LISA) not before 2034 → space borne GW detector for low frequencies (0.1 mHz ... 1 Hz) → supermassive BHs, white dwarfs, ...
- ▶ Pulsar Timing Arrays (ongoing efforts) nanoHertz → supermassive BHs

What's next? - NS mergers?



The image shows a screenshot of a web page from the journal Nature. The page features a dark red header with the 'nature' logo and the tagline 'International weekly journal of science'. Below the header is a navigation menu with links for Home, News & Comment, Research, Careers & Jobs, Current Issue, Archive, Audio & Video, and For Authors. A secondary navigation bar shows the breadcrumb path: News & Comment > News > 2017 > September > Article. The main content area is titled 'NATURE | EXPLAINER' and contains the article title 'Rumours swell over new kind of gravitational-wave sighting'. Below the title is a sub-headline: 'Gossip over potential detection of colliding neutron stars has astronomers in a tizzy.' The author's name, 'Davide Castelvecchi', is listed. The publication date is '24 August 2017' and the update dates are '25 August 2017, 25 August 2017'. A black arrow points to the update dates. A 'Rights & Permissions' button is visible below the text. At the bottom of the page, there is a large image of a star field.

nature International weekly journal of science

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News & Comment > News > 2017 > September > Article

NATURE | EXPLAINER

Rumours swell over new kind of gravitational-wave sighting

Gossip over potential detection of colliding neutron stars has astronomers in a tizzy.

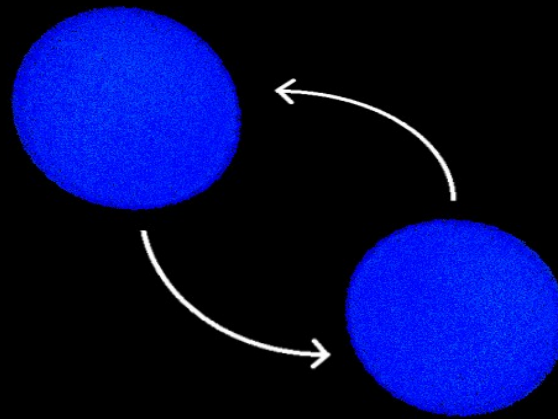
Davide Castelvecchi

24 August 2017 | Updated: 25 August 2017, 25 August 2017

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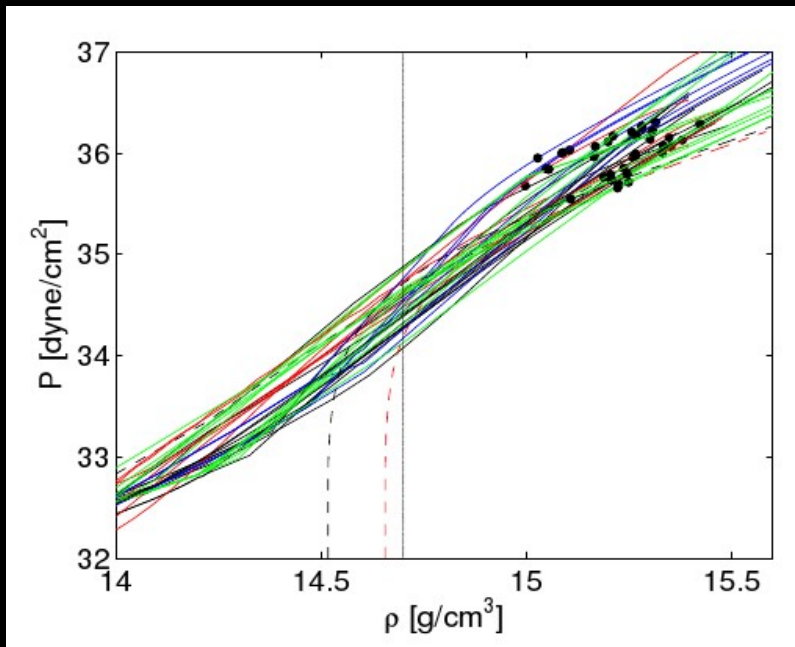


Neutron-star mergers and the nuclear EoS

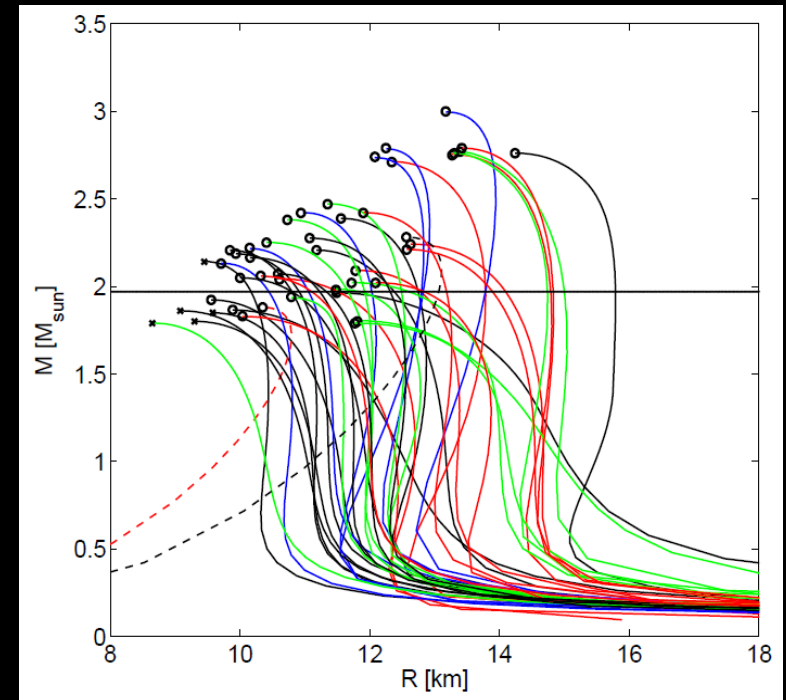


EoS of NS matter

- ▶ Mass-radius relation (of non-rotating NSs) and EoS are uniquely linked through Tolman-Oppenheimer-Volkoff (TOV) equations



TOV
↔



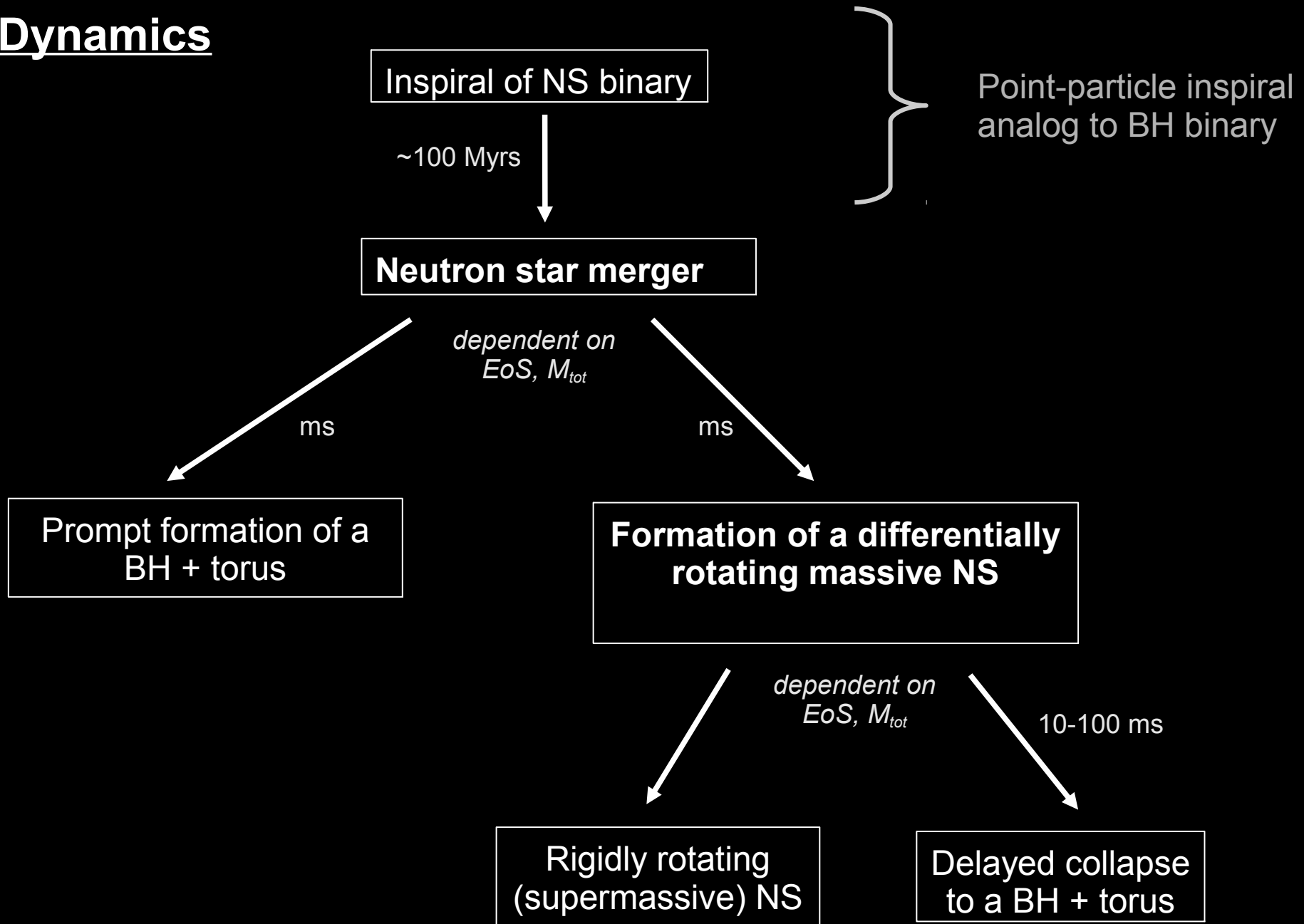
Theory: $P(\rho)$ ↔ currently
future Observation: $R(M)$

=> NS properties (of non-rotating stars) and EoS properties are equivalent !!!

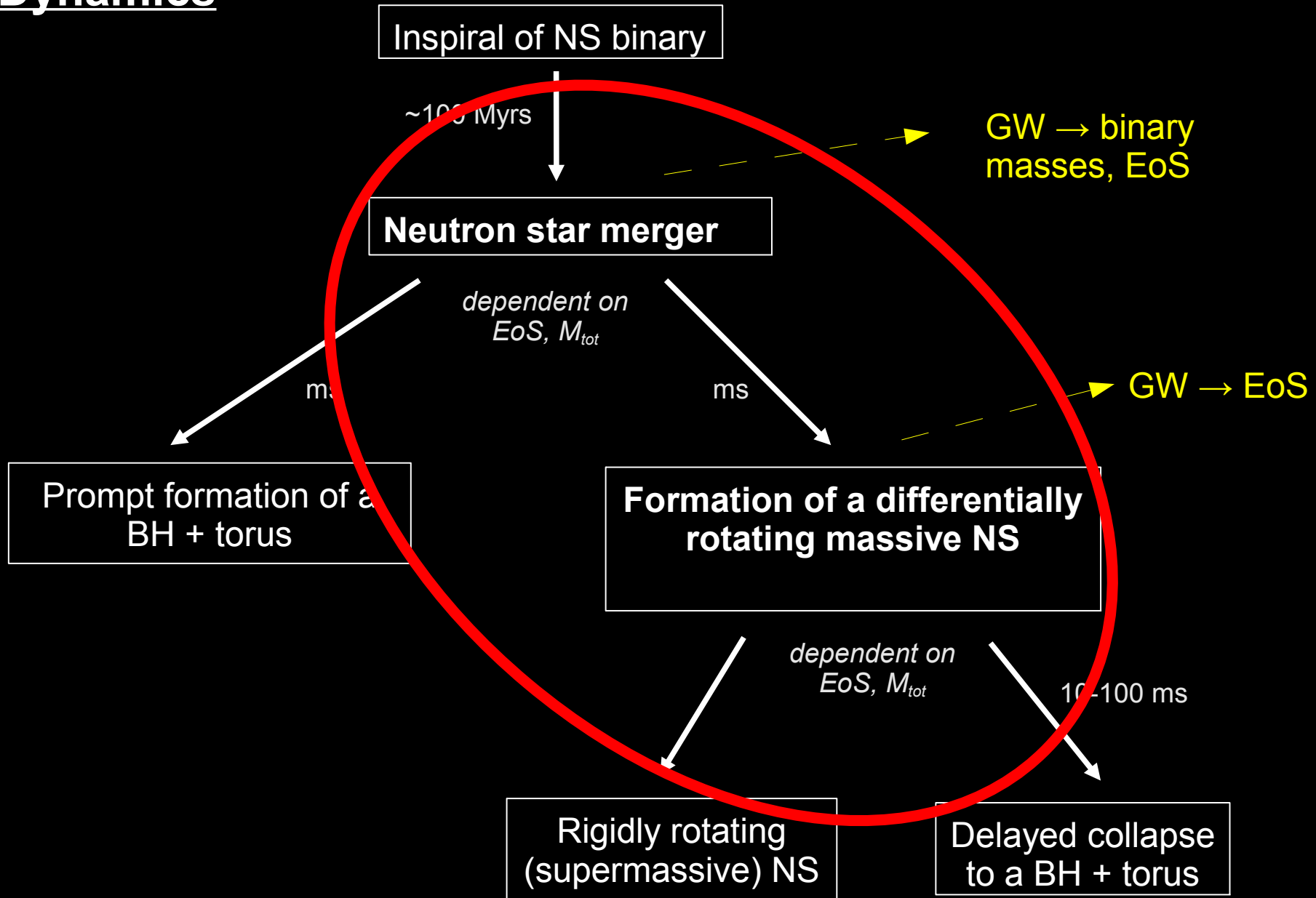
=> in particular we would like to measure radius of fixed mass, e.g. $R_{1.35}$, $R_{1.6}$

Merger stages

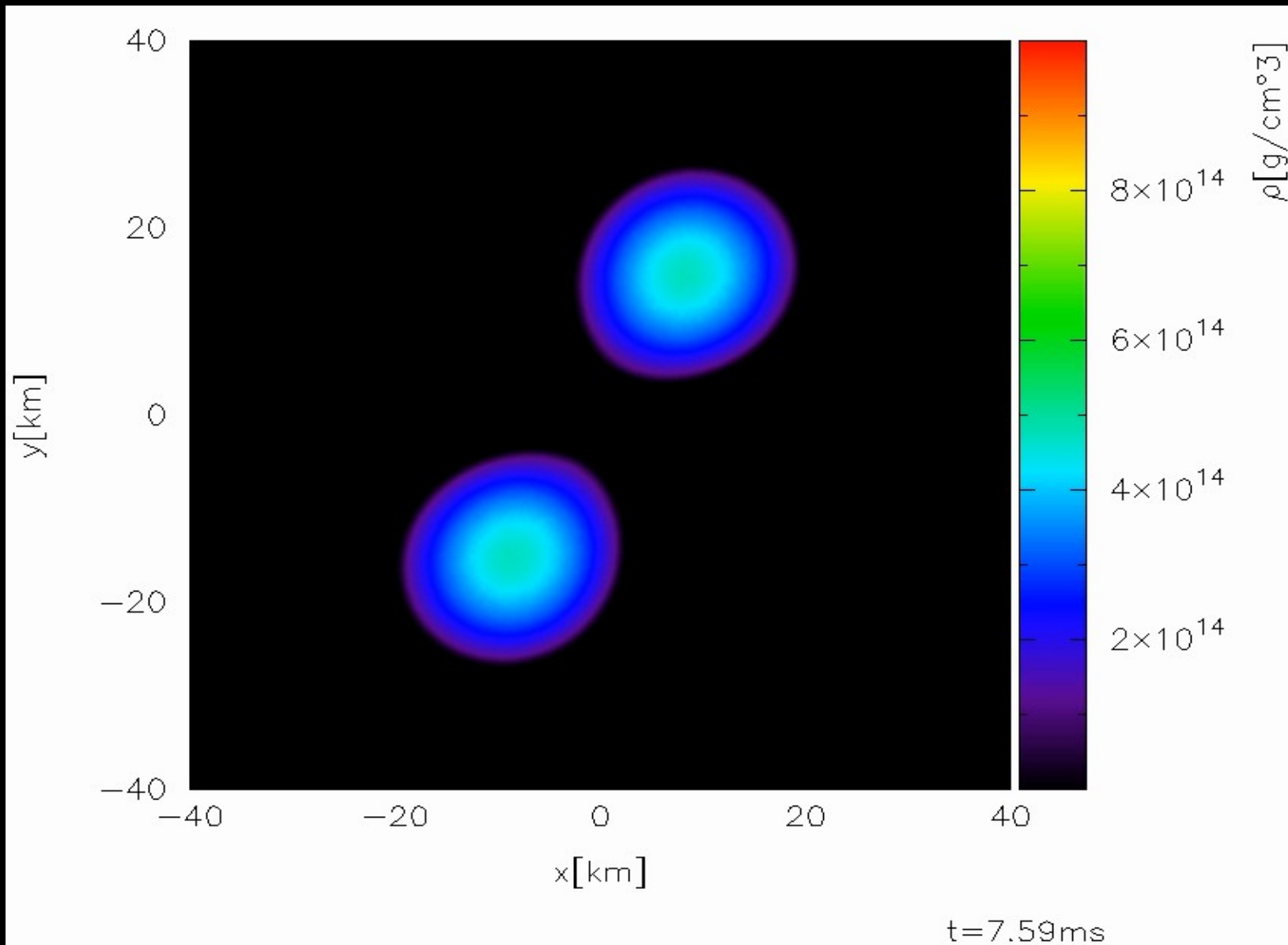
Dynamics



Dynamics

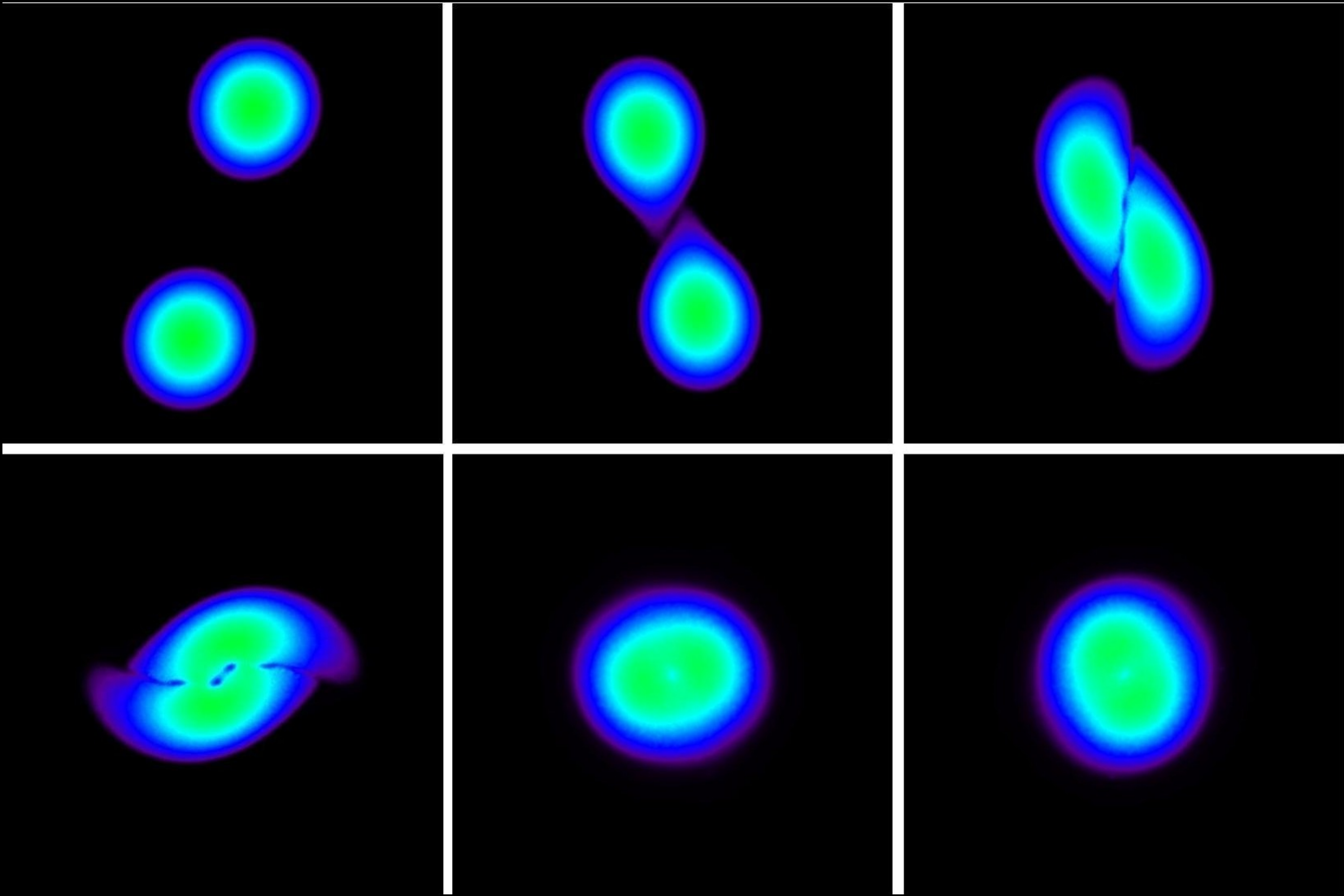


Simulation: 1.35+1.35 M_{sun}



Density evolution in equatorial plane, Shen EoS

Only late inspiral phase and (post-)merger phase covered by simulation



Goal: EoS from GWs

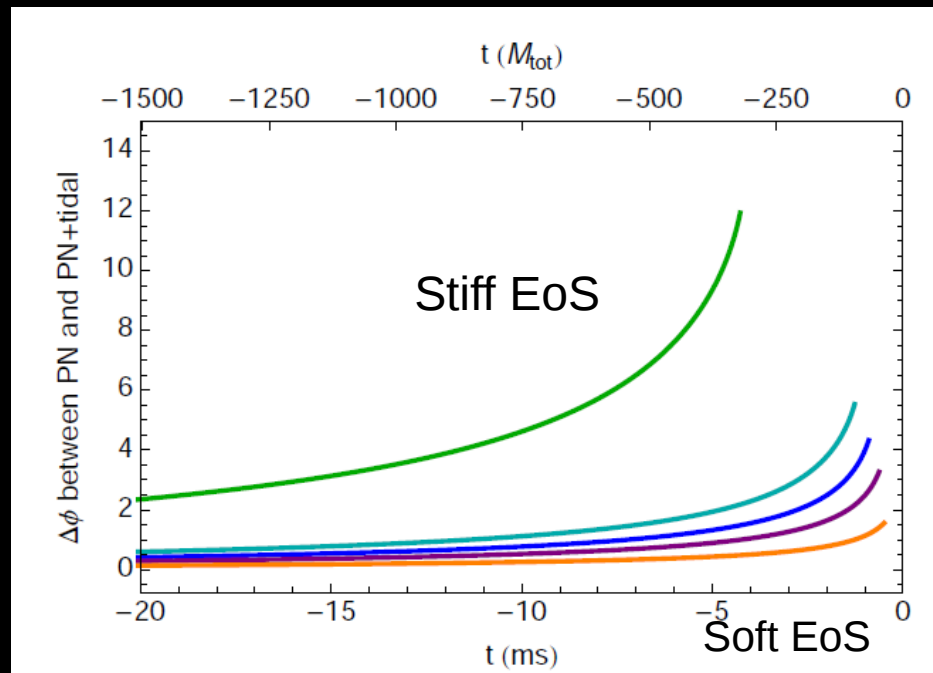
Two complementary strategies:

- ▶ Tidal effects during the inspiral → accelerate inspiral compared to BH-BH
 - strong signal – weaker EoS effect
- ▶ Oscillations of the postmerger remnant
 - strong EoS impact – weaker signal (at higher frequencies)
- ▶ Keep in mind: binary masses are easy to measure

EoS effects during inspiral

Inspiral

- ▶ Orbital phase evolution affected by NS radius (precisely tidal deformability) – only during last orbits before merging
- ▶ Difference in phase between NS merger and point-particle inspiral:



e.g. Read et al. 2013

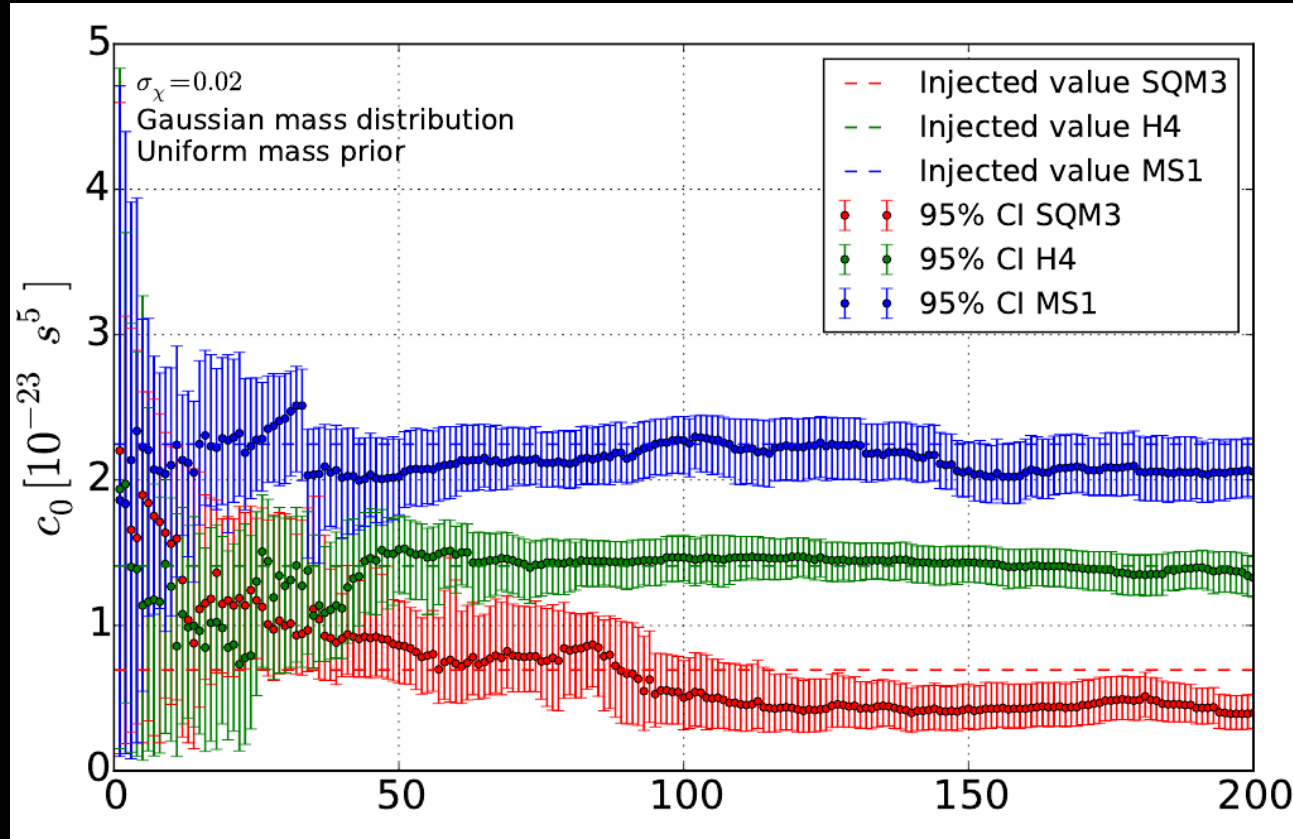
Merger time of point particle

EoS impact measured by tidal deformability

$$\lambda(M) = \frac{2}{3} k_2(M) R^5$$

Challenge: construct faithful templates for data analysis

Tidal deformability – combining many signals

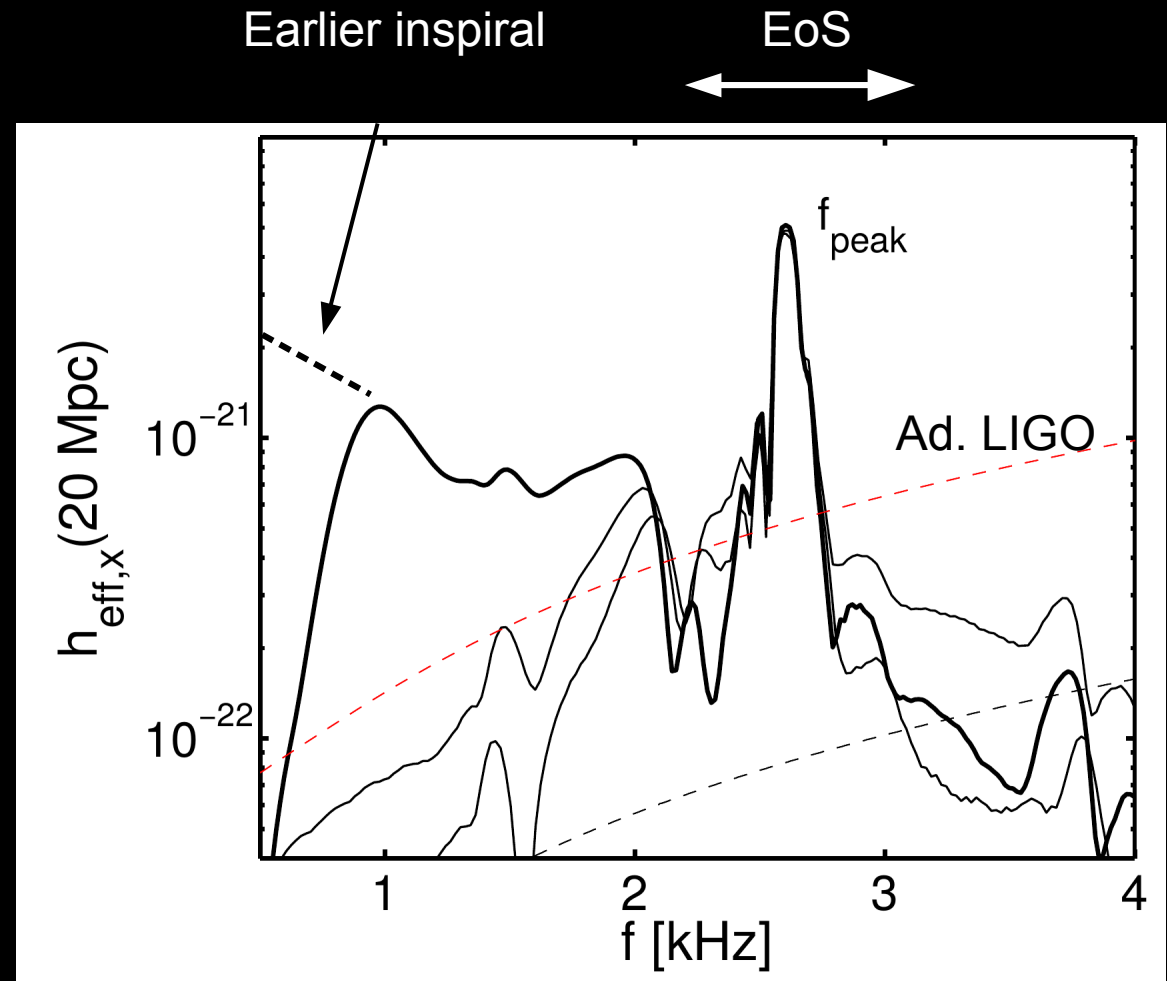
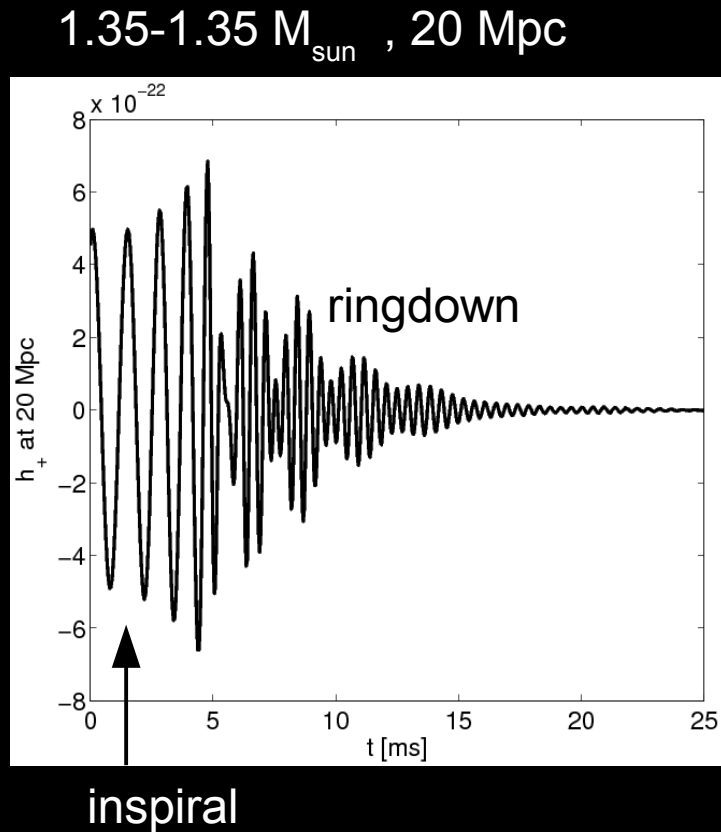


$$\lambda(m) \simeq c_0 + c_1 \left(\frac{m - m_0}{M_\odot} \right) + \frac{1}{2} c_2 \left(\frac{m - m_0}{M_\odot} \right)^2$$

Agathos et al. 2015

Radius measurements from the postmerger phase

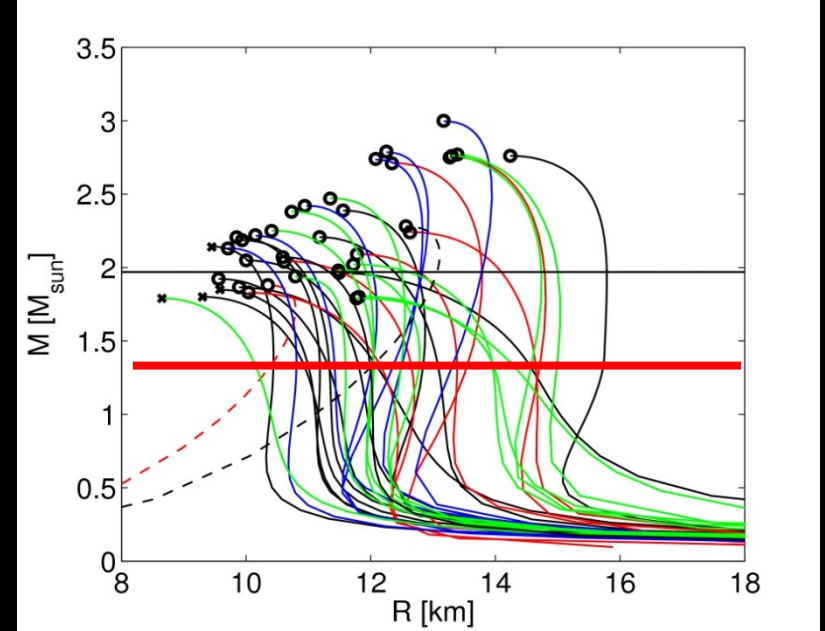
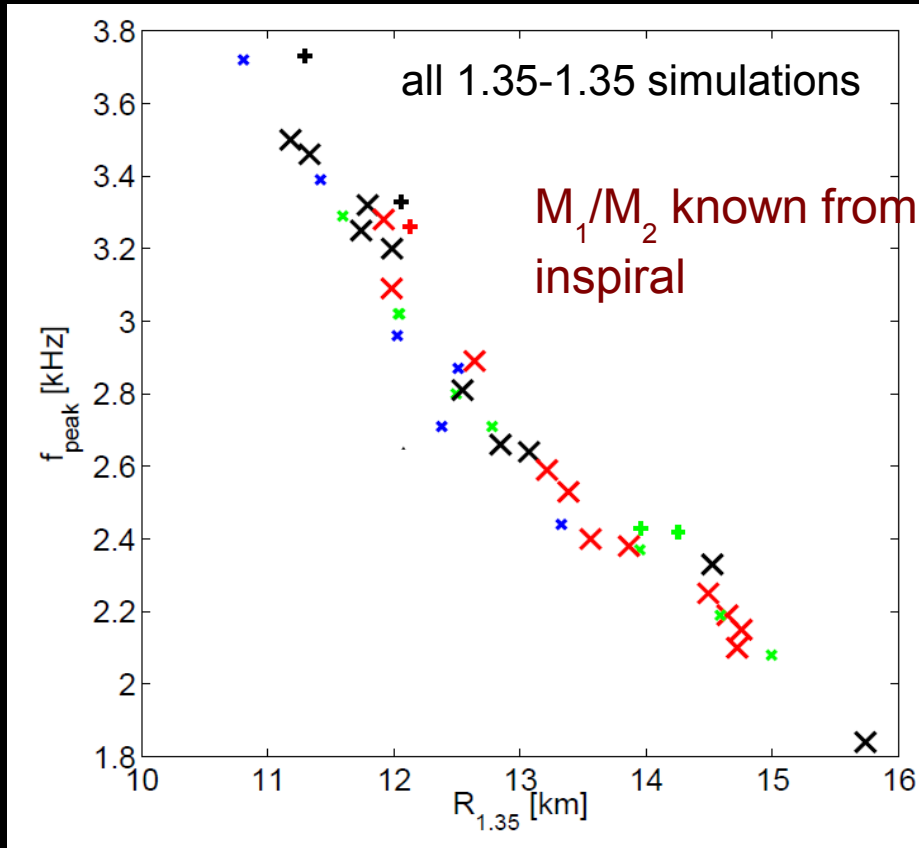
Postmerger



Dominant postmerger oscillation frequency f_{peak}

Very characteristic (robust feature in all models)

Every data point a single simulation of a $1.35-1.35 M_{\text{sun}}$ binary



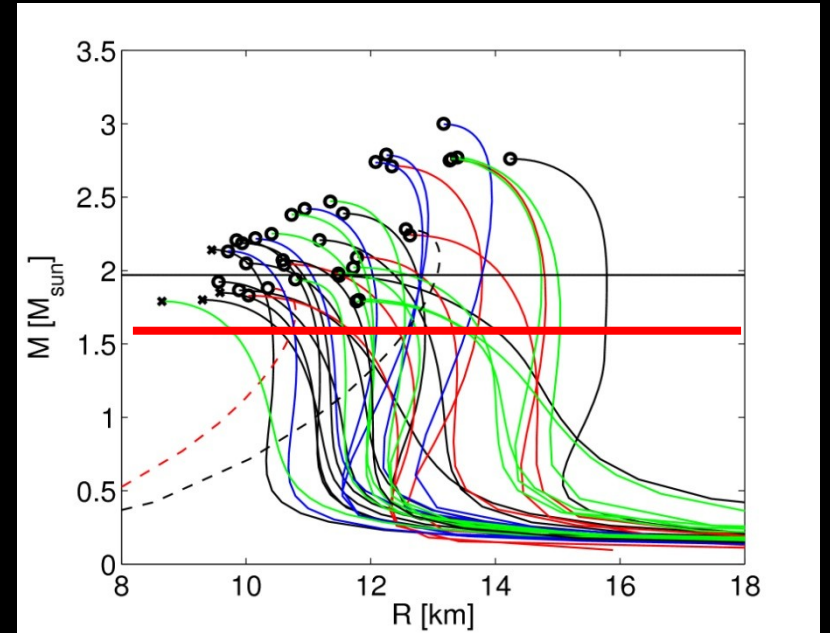
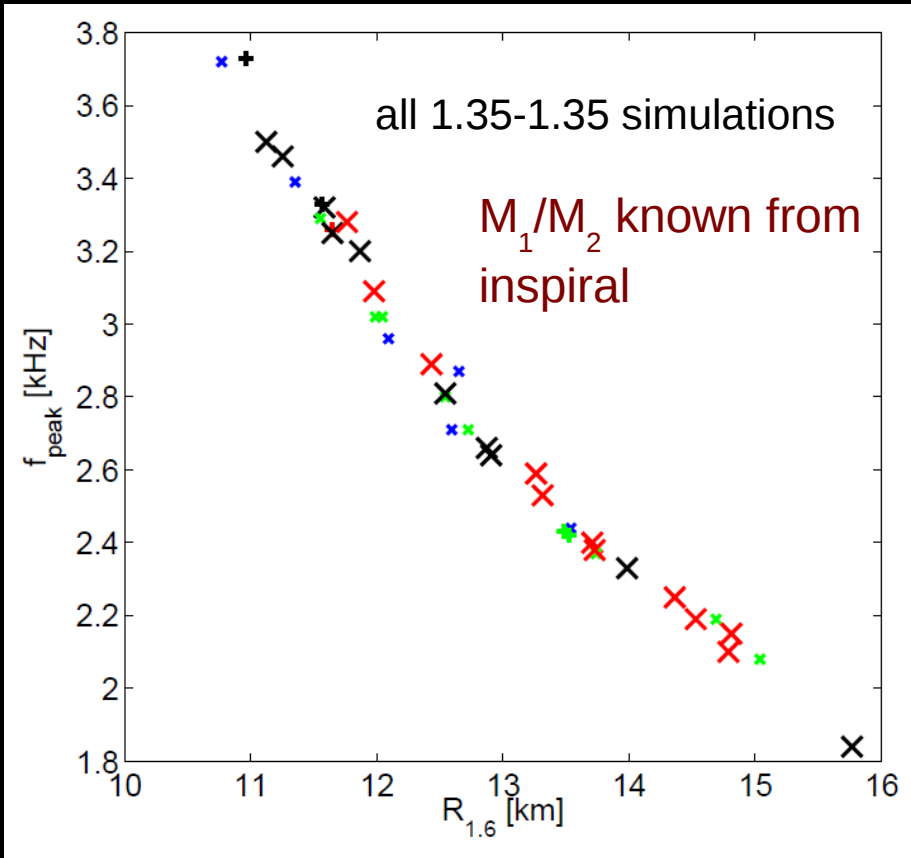
characterize EoS by radius of nonrotating NS with $1.35 M_{\text{sun}}$

Bauswein et al. 2012

Pure TOV property => **Radius measurement** via f_{peak}

→ **Empirical relation between GW frequency and NS radius (= our EoS parameter)**

Important: Simulations for the same binary mass, but with varied EoS



characterize EoS by radius of nonrotating NS with $1.6 M_{\text{sun}}$

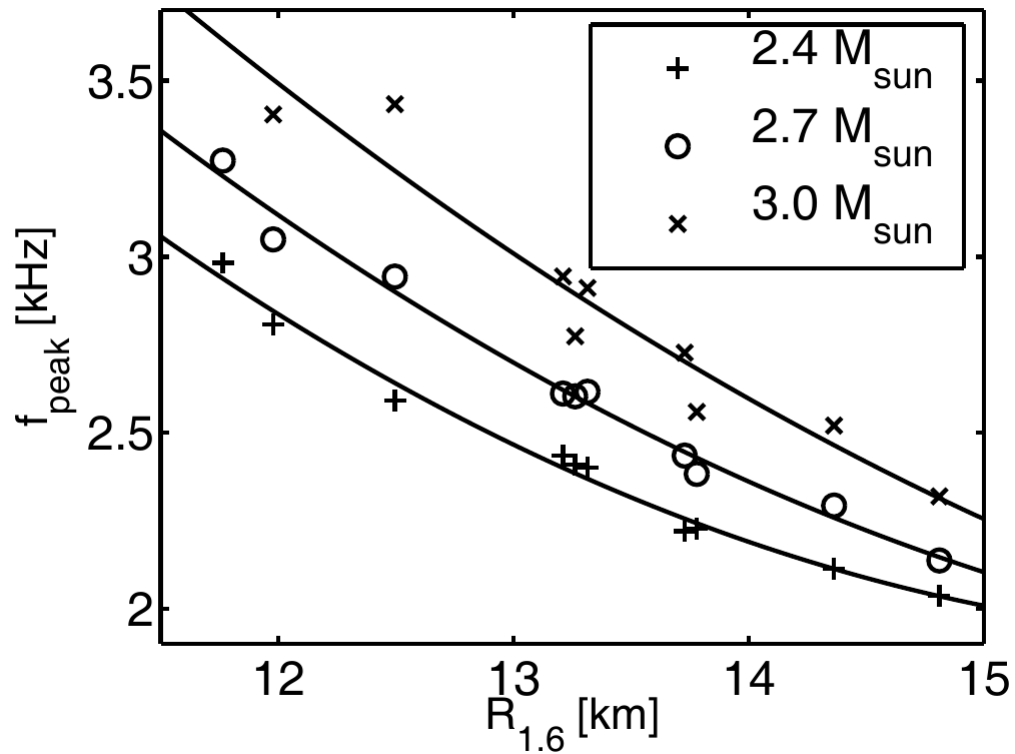
Bauswein et al. 2012

Pure TOV/EoS property => **Radius measurement** via f_{peak}

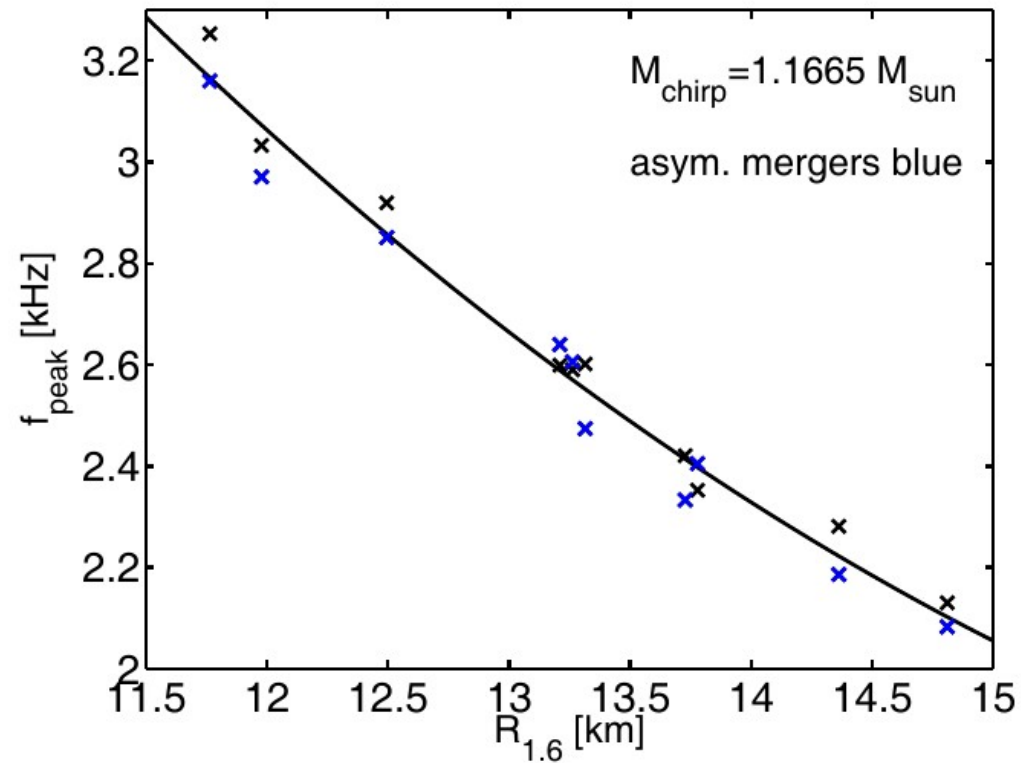
Fit: $R(1.6 M_{\odot}) = 1.1 f_{GW}^2 - 8.6 f_{GW} + 28.$

Important: Simulations for the same binary mass, just with varied EoS

Binary mass variations



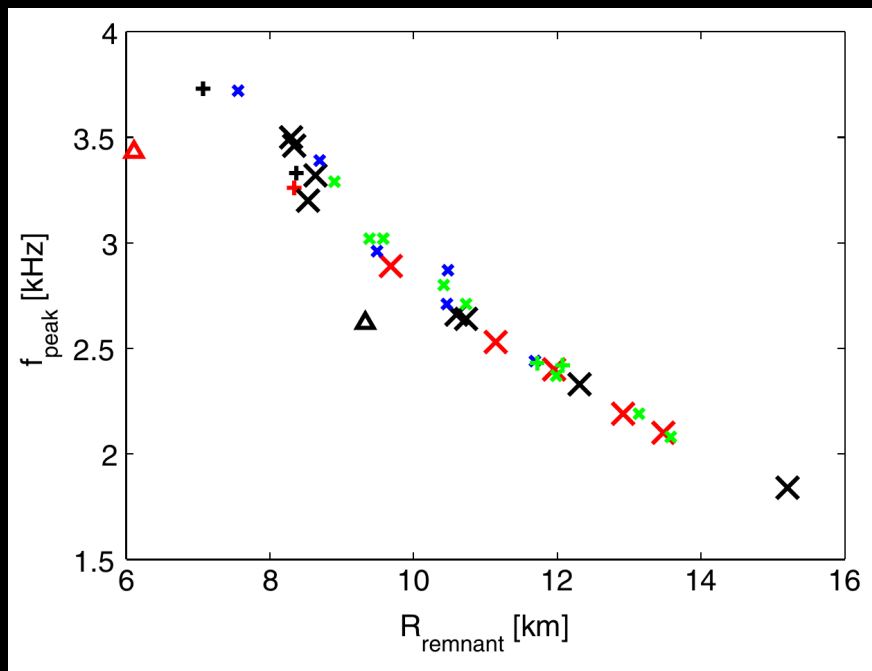
Different total binary masses
(symmetric)



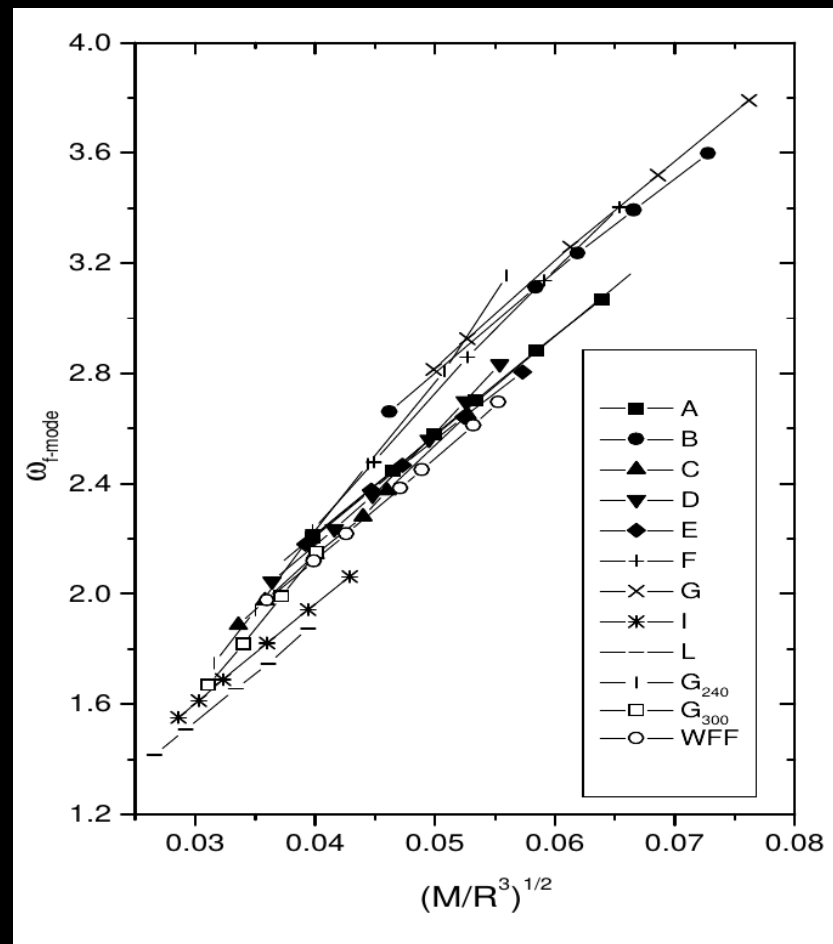
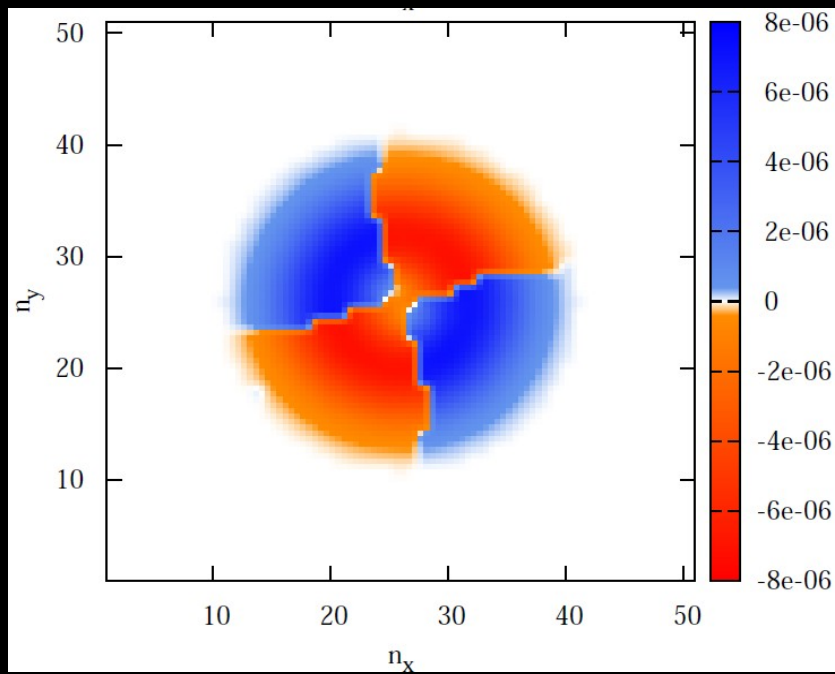
Fixed chirp mass (asymmetric 1.2-1.5
 M_{sun} binaries and symmetric 1.34-
1.34 M_{sun} binaries)

► Background

Bauswein et al. 2012



Stergioulas et al. 2011



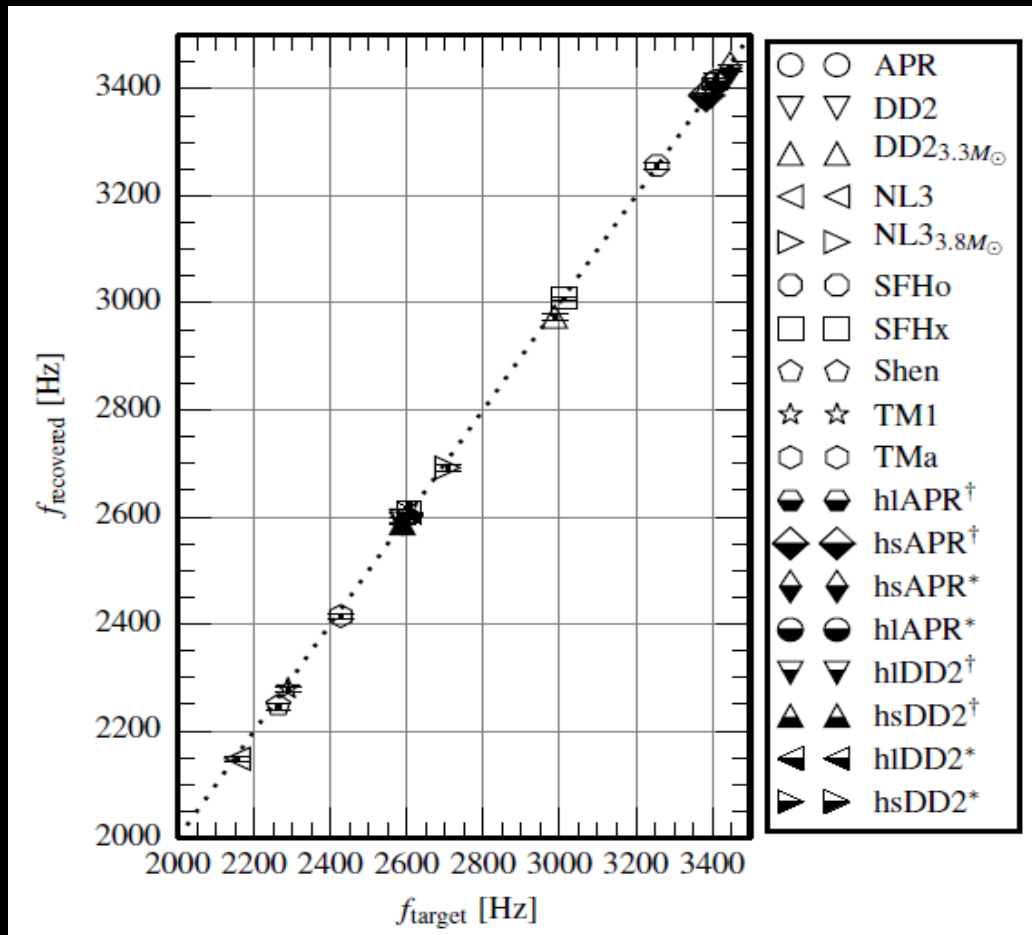
Andersson & Kokkotas 1998

f-mode frequency of nonrotating stars:

$$f \propto \sqrt{\frac{M}{R^3}}$$

Data analysis

Data analysis – prove of principle



Model waveforms hidden in rescaled LIGO noise

Peak frequency recovered with burst search analysis

Error ~ 10 Hz

For signals within ~10-25 Mpc

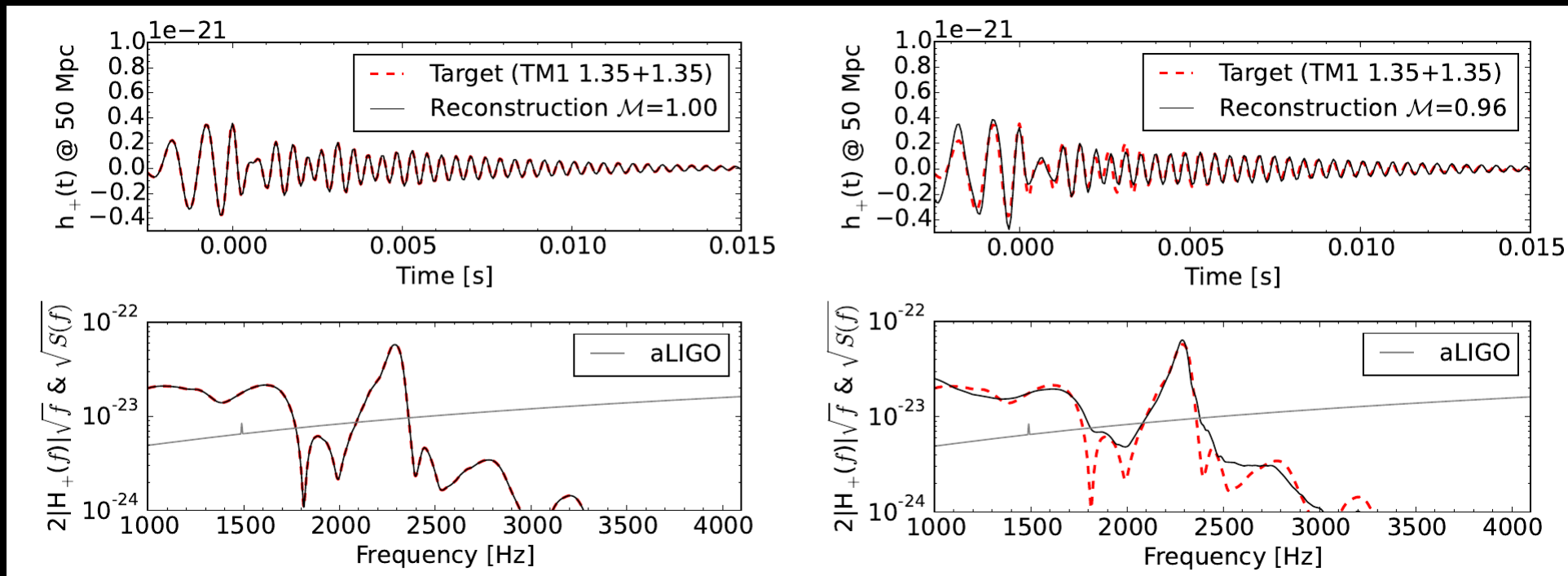
=> for near-by event radius measurable with high precision (~0.01-1/yr)

Proof-of-principle study
→ improvements likely

Clark et al. 2014

Data analysis

► Principal Component analysis



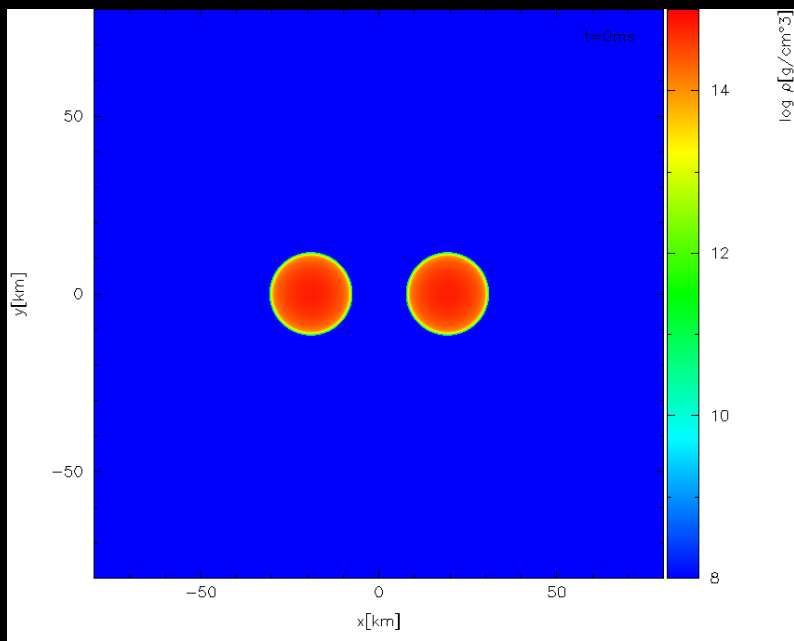
Excluding recovered waveform from catalogue

Clark et al. 2016

(stacking results, e.g. Yang et al., Bose et al.)

Instrument	SNR_{full}	D_{hor} [Mpc]	$\dot{\mathcal{N}}_{\text{det}}$ [year $^{-1}$]
aLIGO	2.99 ^{3.86} _{2.37}	29.89 ^{38.57} _{23.76}	0.01 ^{0.03} _{0.01}
A+	7.89 ^{10.16} _{6.25}	78.89 ^{101.67} _{62.52}	0.13 ^{0.20} _{0.10}
LV	14.06 ^{18.13} _{11.16}	140.56 ^{181.29} _{111.60}	0.41 ^{0.88} _{0.21}
ET-D	26.65 ^{34.28} _{20.81}	266.52 ^{342.80} _{208.06}	2.81 ^{5.98} _{1.33}
CE	41.50 ^{53.52} _{32.99}	414.62 ^{535.22} _{329.88}	10.59 ^{22.78} _{5.33}

Collapse behavior of the merger remnant

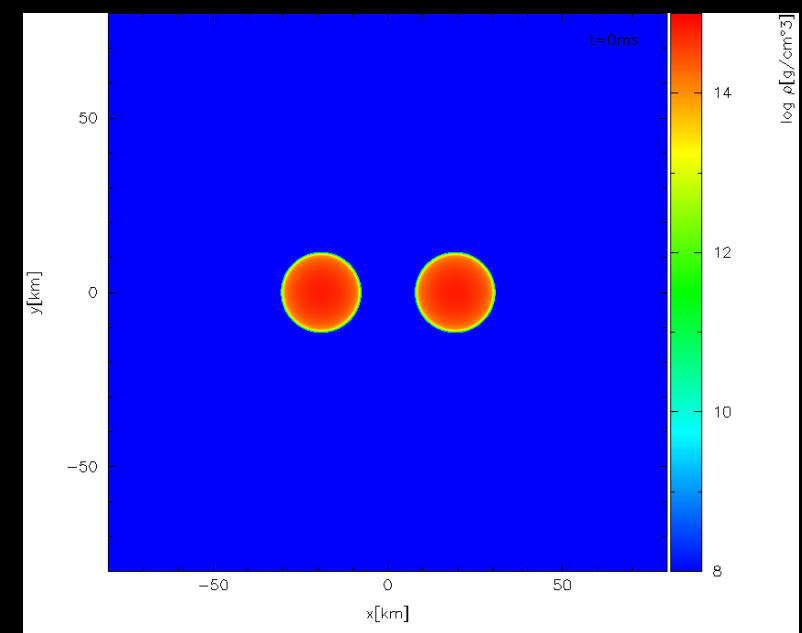


$$M_{\text{tot}} = 3.4 M_{\odot}$$



Shen EoS

$$M_{\text{tot}} = 3.5 M_{\odot}$$



Collapse behavior:

Prompt vs. delayed (/no) collapse

Relevant for:

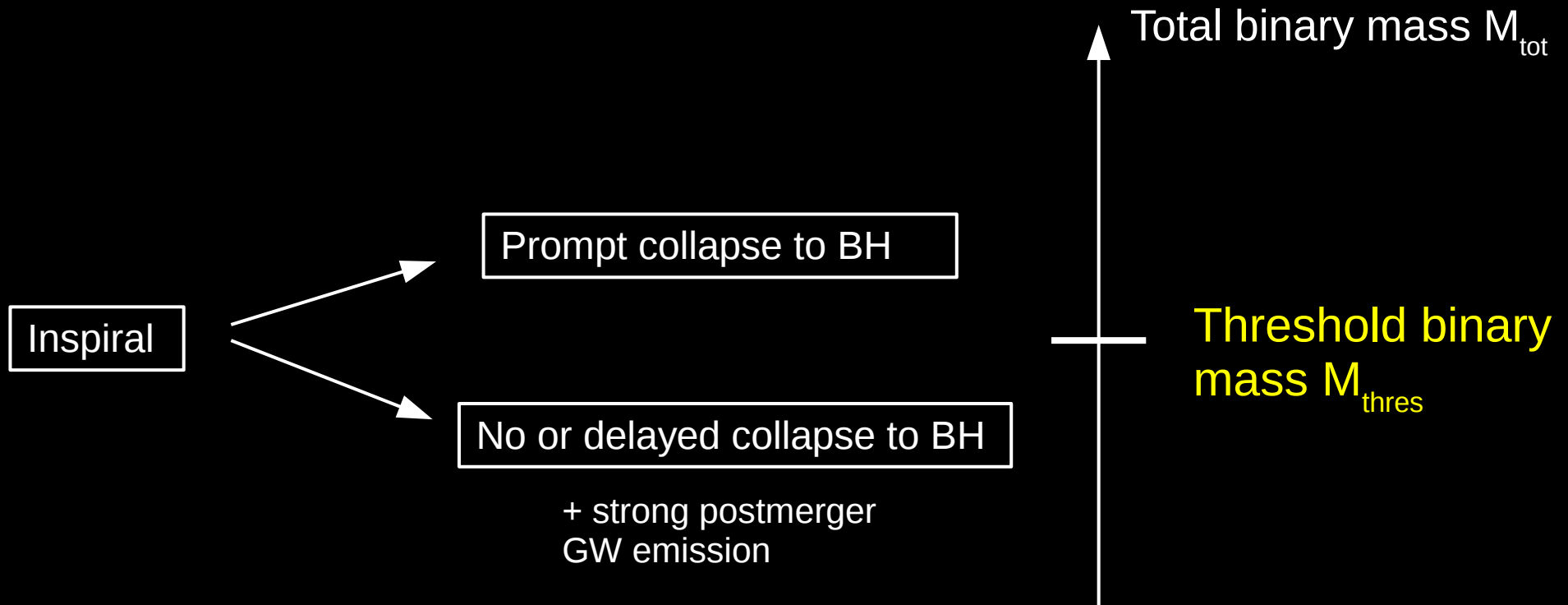
EoS constraints through M_{max} measurement

Conditions for short GRBs

Mass ejection

Electromagnetic counterparts powered by thermal emission

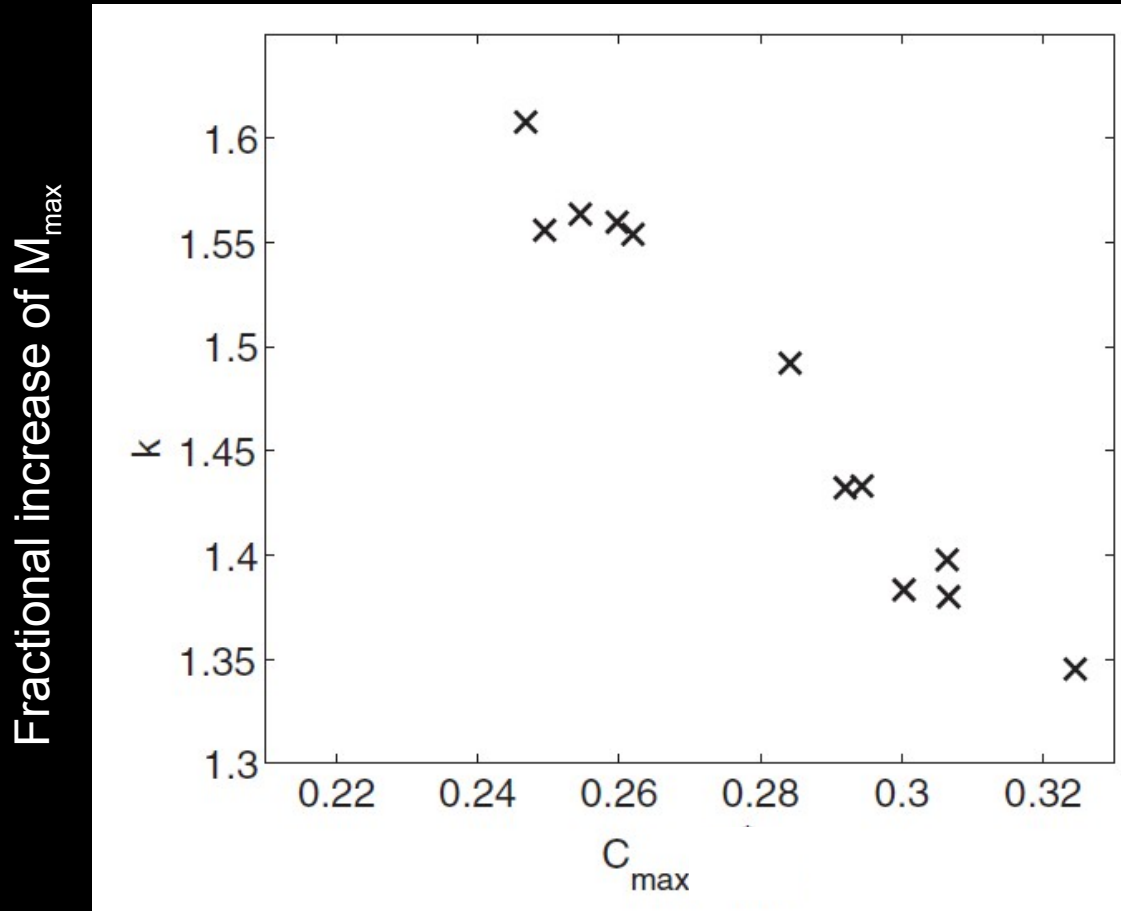
Collapse behavior



EoS dependent - somehow M_{max} should play a role

→ ... from observations we can determine M_{max} , R_{max} , ρ_{max}

Key quantity: **Threshold binary mass M_{thres}** for prompt BH collapse



$$M_{\text{thres}} = k * M_{\text{max}}$$

with $k = k(C_{\text{max}})$

$$C_{\text{max}} = G M_{\text{max}} / (c^2 R_{\text{max}})$$

(compactness of TOV maximum-mass configuration)

$$\Rightarrow M_{\text{thres}} = M_{\text{thres}}(M_{\text{max}}, R_{\text{max}})$$

Bauswein et al. 2013

$$k = \frac{M_{\text{thres}}}{M_{\text{max}}}$$

← From simulations with different M_{tot}

← TOV property of employed EoS

Constrain M_{\max}

- ▶ Measure several NS mergers with different M_{tot} – check if postmerger GW emission present

→ M_{thres} estimate

- ▶ Radius e.g. from postmerger frequency

$$M_{\text{thres}} = \left(-3.38 \frac{GM_{\max}}{c^2 R_{\max}} + 2.43 \right) M_{\max}$$

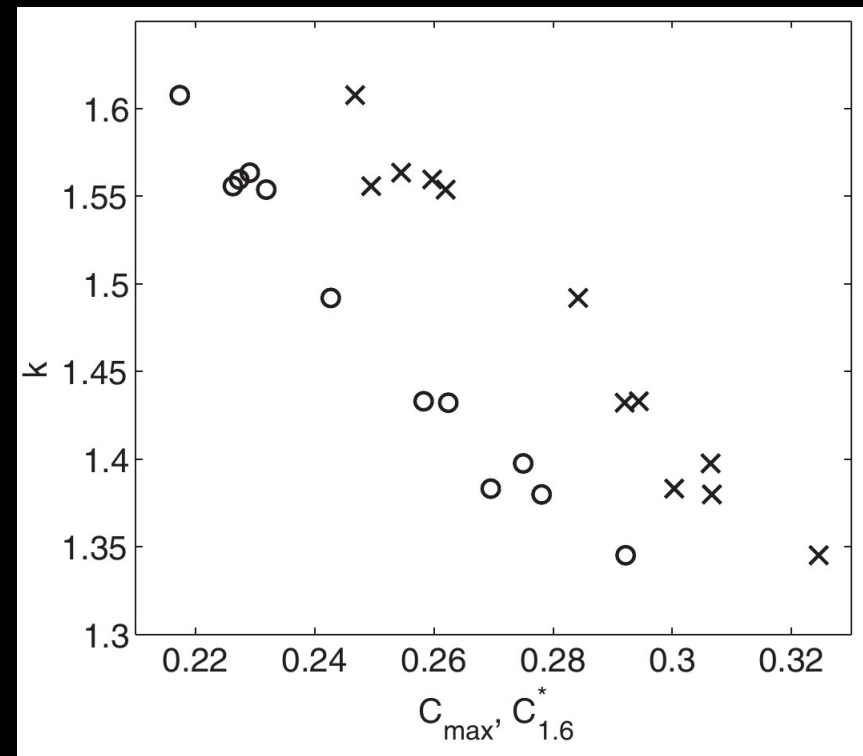
- ▶ Invert fit

$$M_{\text{thres}} = \left(-3.6 \frac{GM_{\max}}{c^2 R_{1.6}} + 2.38 \right) M_{\max}$$

→ M_{\max}

- ▶ Note: already a single/few measurement could provide interesting constraints !!!

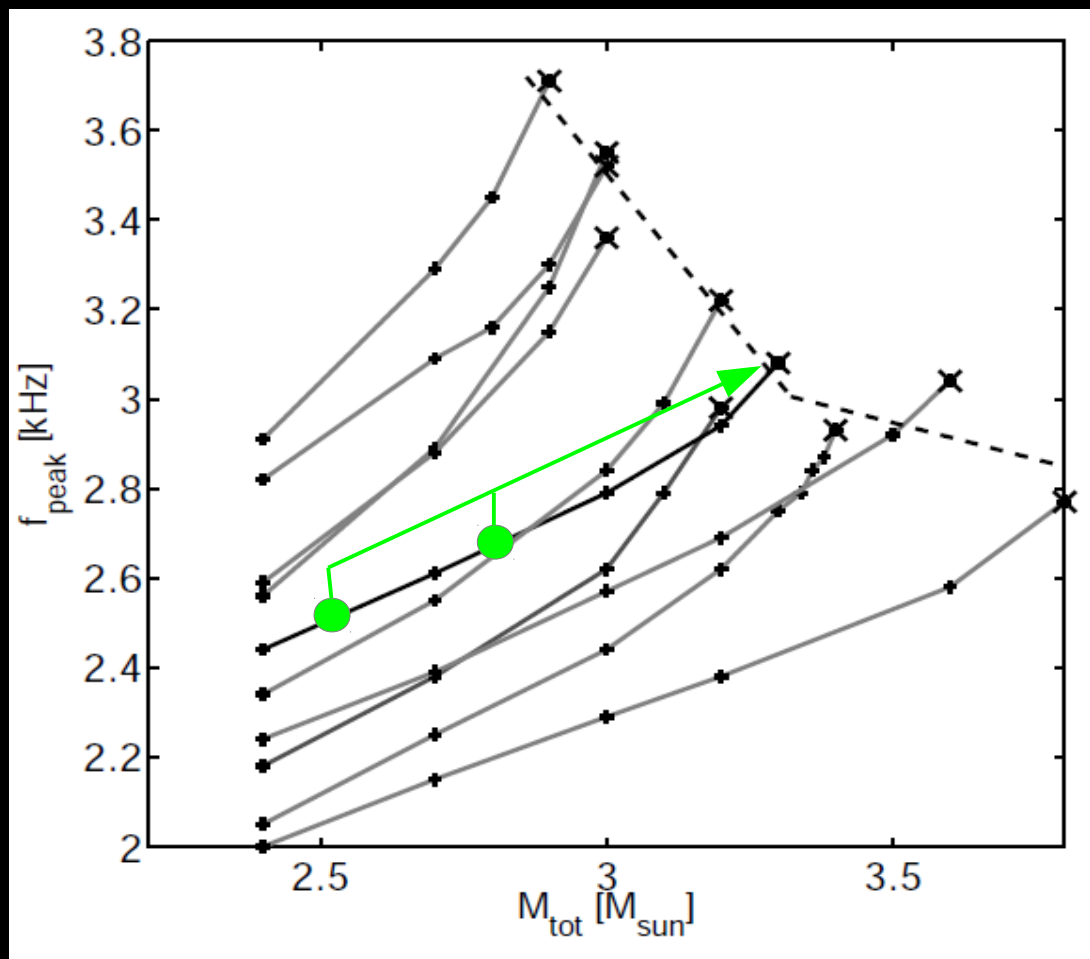
- ▶ M_{thres} constraints also from GRB, em counterparts, ...



One more idea:

maybe we get more events but not with high binary masses

Alternative: f_{peak} dependence on total binary mass



(every single line corresponds to a specific EoS
→ only one line can be the true EoS)

$$f_{peak} \sim \sqrt{\frac{M}{R^3}}$$

Bauswein et al. 2014

Dominant GW frequency monotone function of M_{tot}

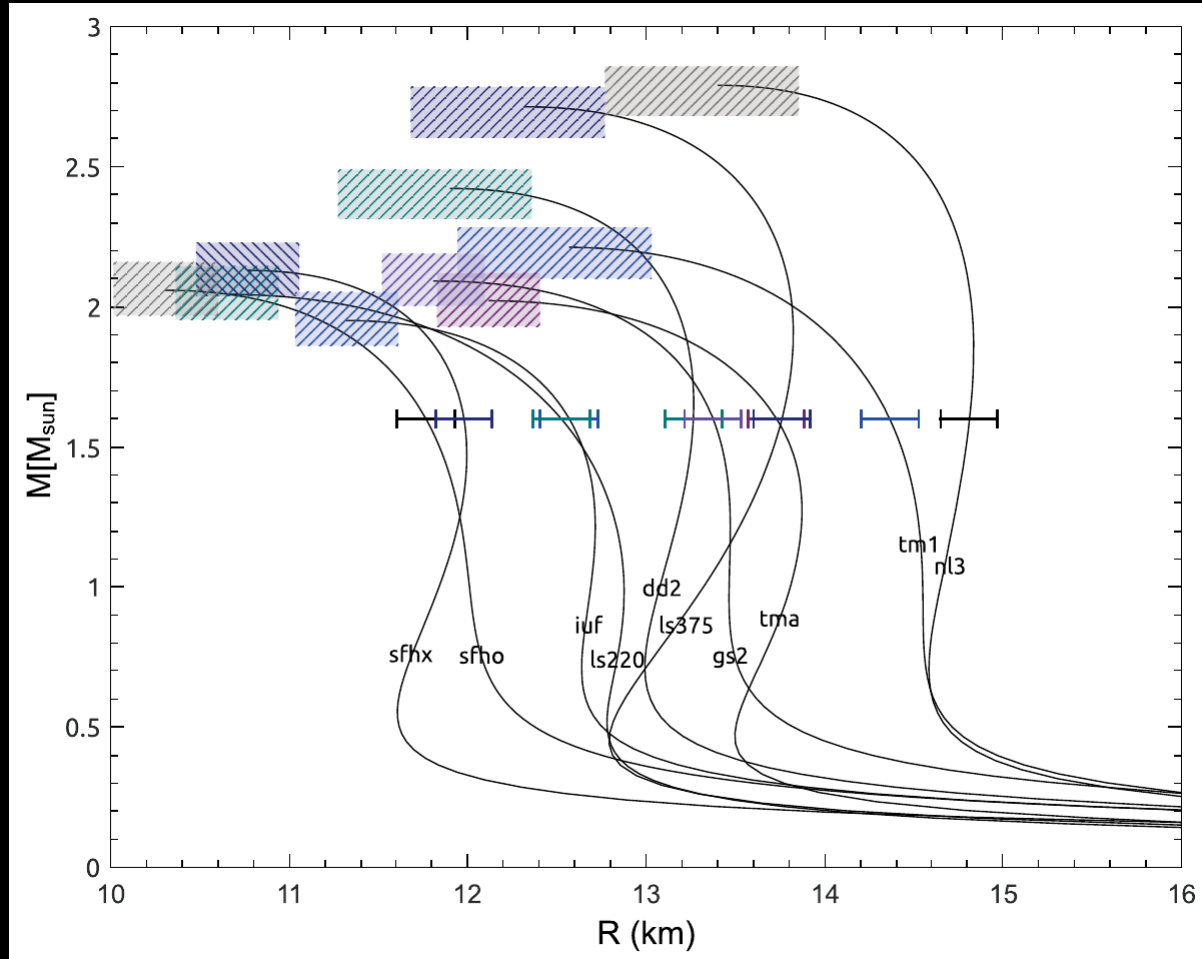
Threshold to prompt BH collapse shows a clear dependence on M_{tot}
(dashed line)

from two measurements of f_{peak} at moderate M_{tot}

Maximum-mass
TOV properties



by extrapolation
of f_{peak} (M_{tot}



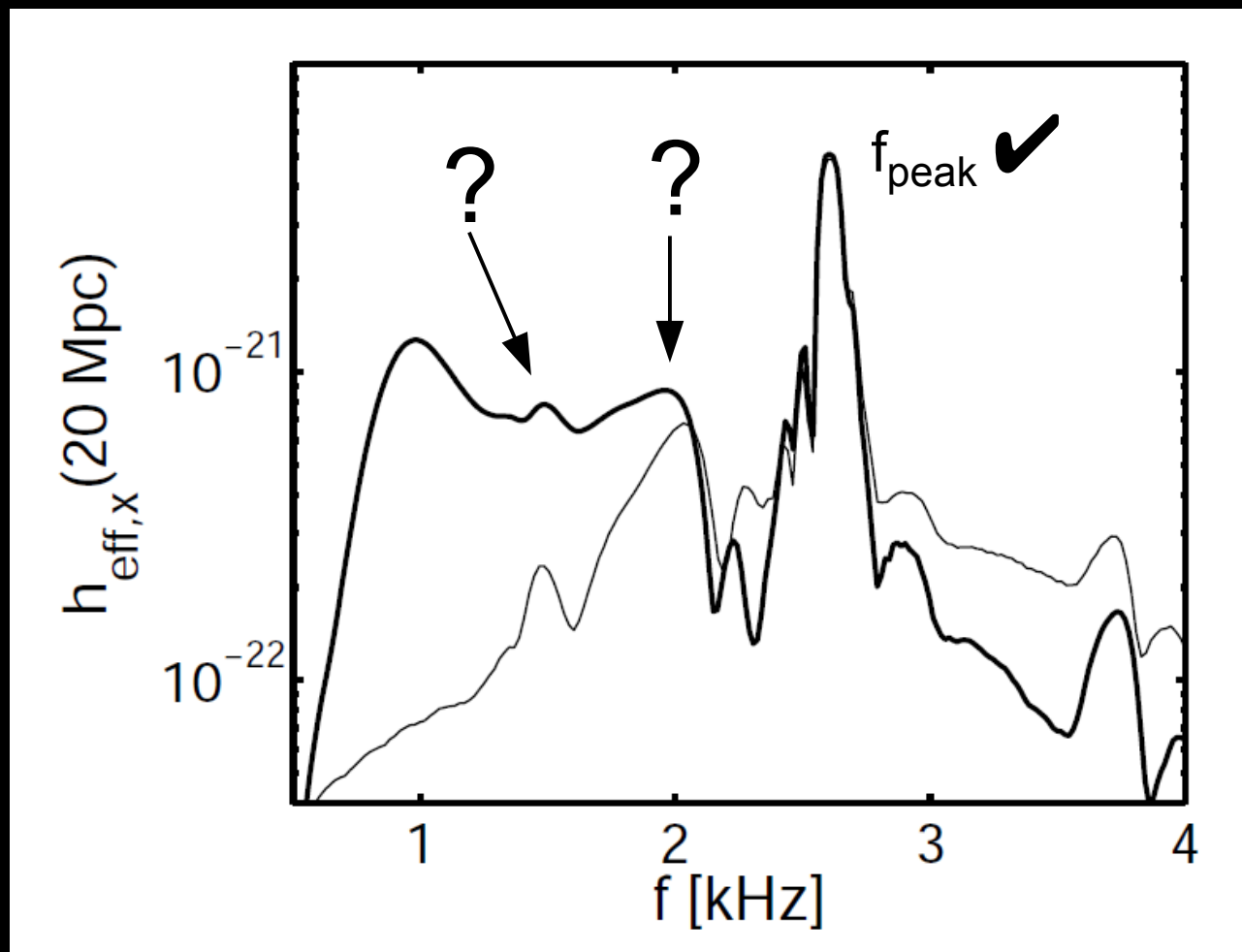
Radius at
lower
masses
from f_{peak}

(final error will depend on EoS and exact systems measured)

Note: M_{thres} may also be constrained from prompt collapse directly

Outlook:
GW astereoseismology

Generic GW spectrum

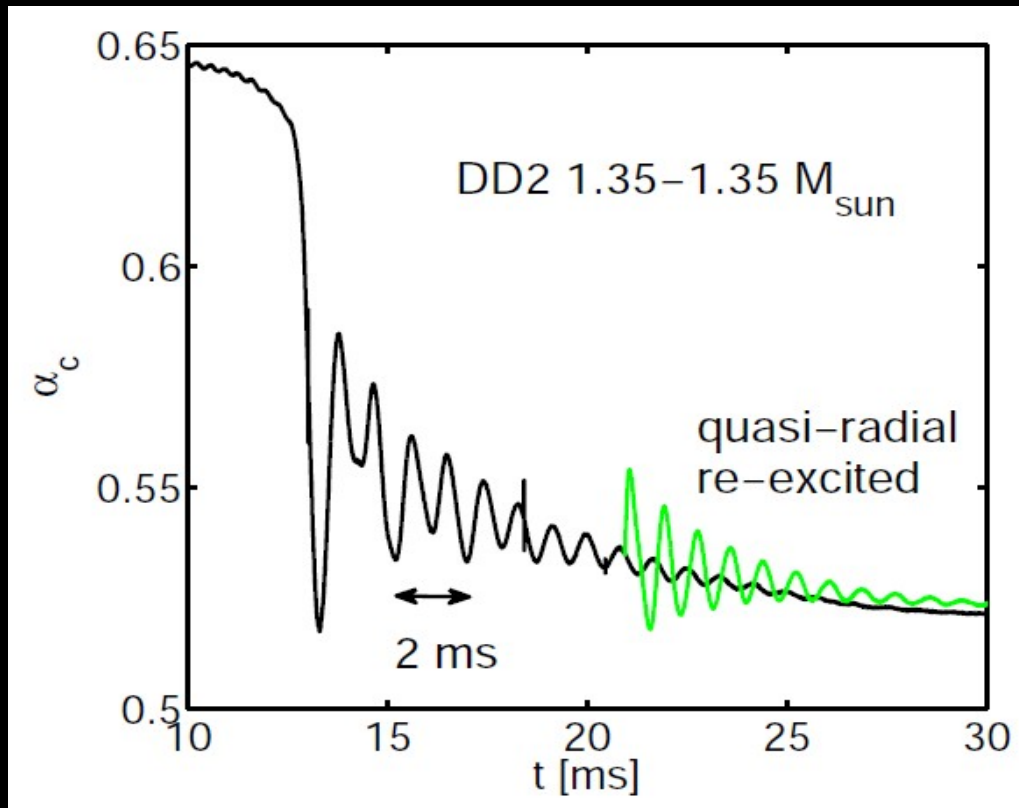


- **Up to three pronounced features** in the postmerger spectrum (+ structure at higher frequencies)
- 1.35-1.35 M_{sun} DD2 EoS

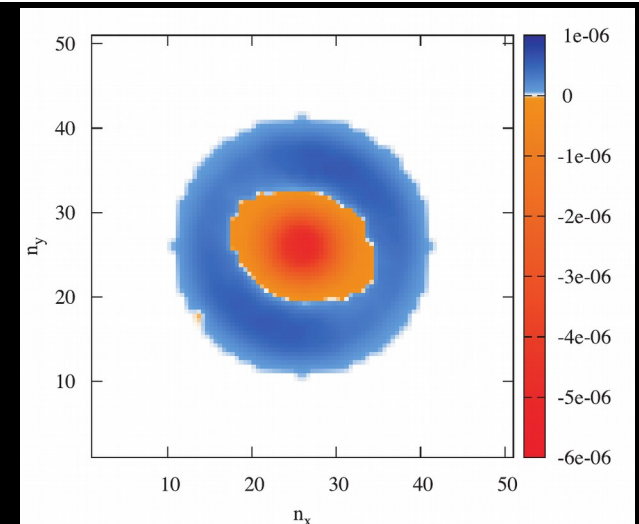
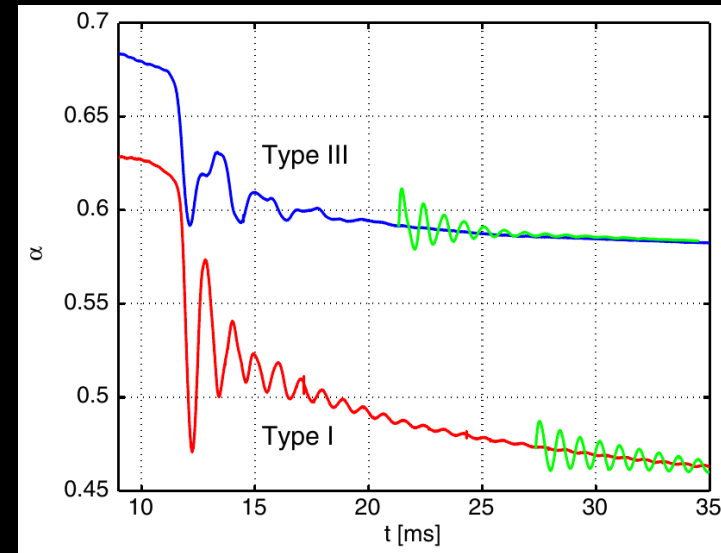
Interpretation and exact dependencies of secondary frequencies still under debate (cf. Frankfurt group)

Quasi-radial mode

- Central lapse function shows two frequencies (~ 500 Hz and ~ 1100 Hz) \rightarrow clear peaks in FFT
- Add quasi-radial perturbation \rightarrow re-excite quasi-radial mode $\Rightarrow f_0 = 1100$ Hz
- Confirmed by mode analysis \rightarrow radial eigen function at f_0



Bauswein et al. 2015

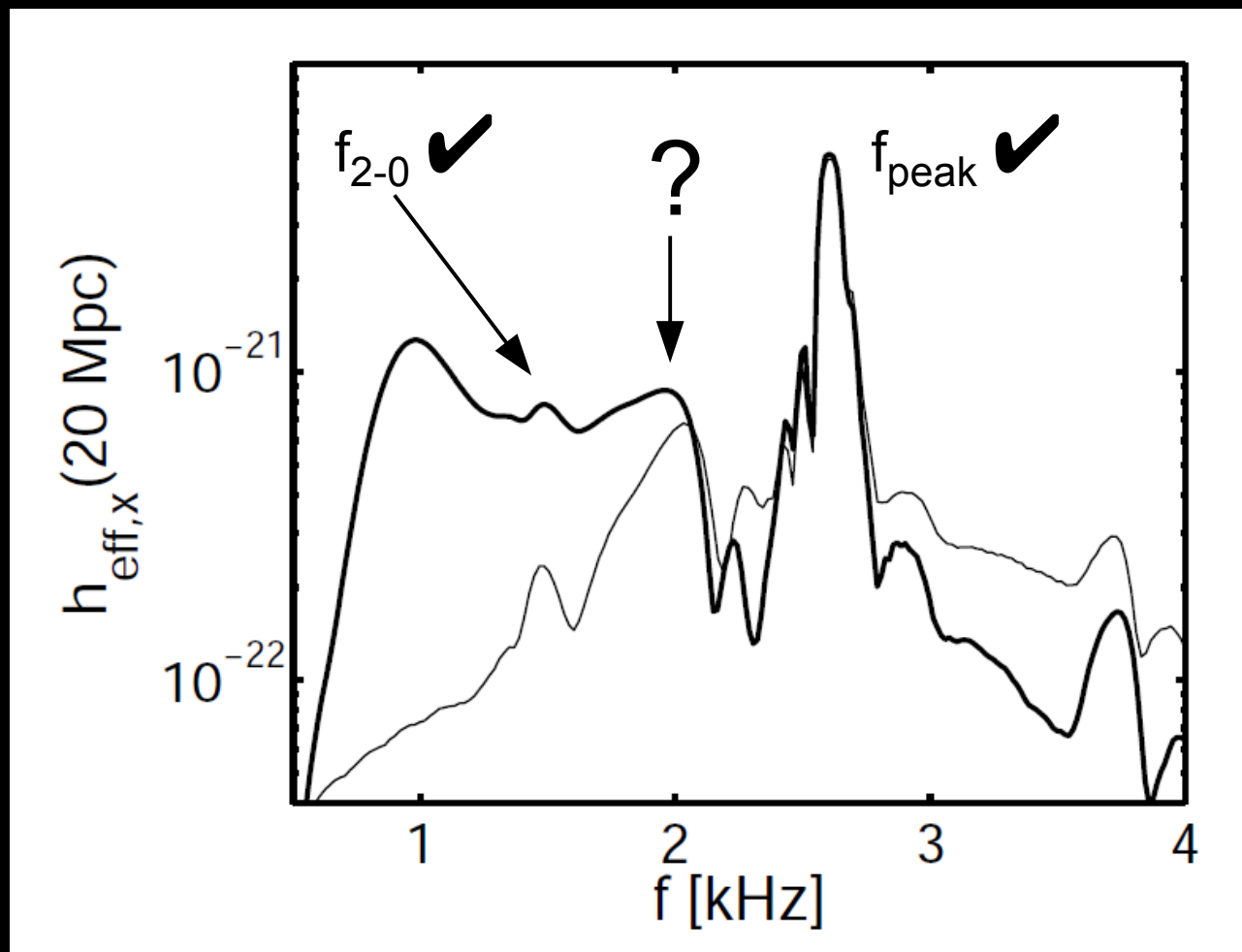


Stergioulas et al. 2011

Could consider also size of the remnant, ρ_{max} , ...

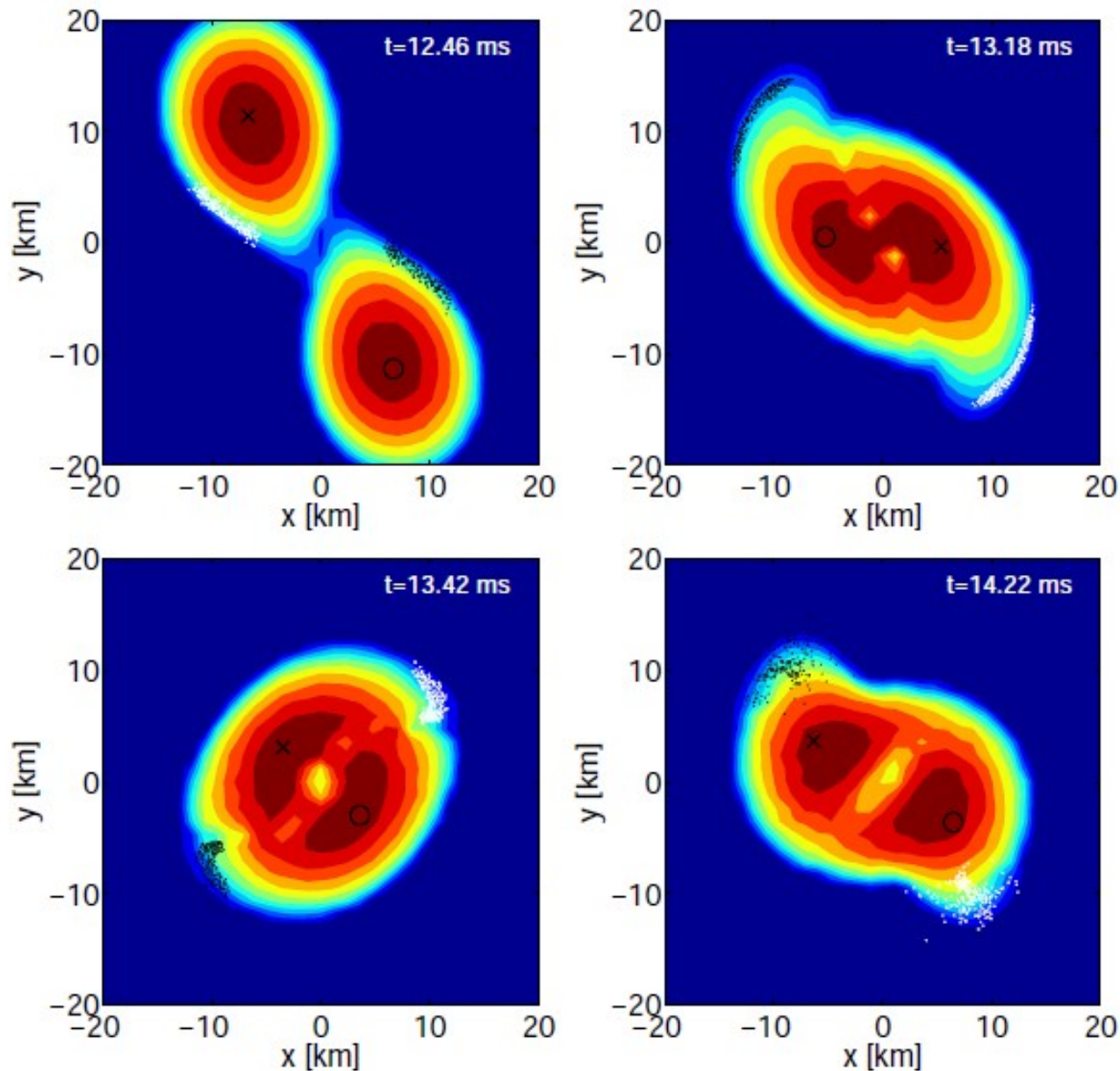
Note: **additional low-frequency oscillation** (500 Hz) also in GW amplitude (explained later)

Generic GW spectrum



- Interaction between dominant quadrupolar mode and quasi-radial oscillation produced peak at $f_{2-0} = f_{\text{peak}} - f_0$ (see Shibata & Taniguchi 2006, Stergioulas et al. 2011)

Antipodal bulges (spiral pattern)



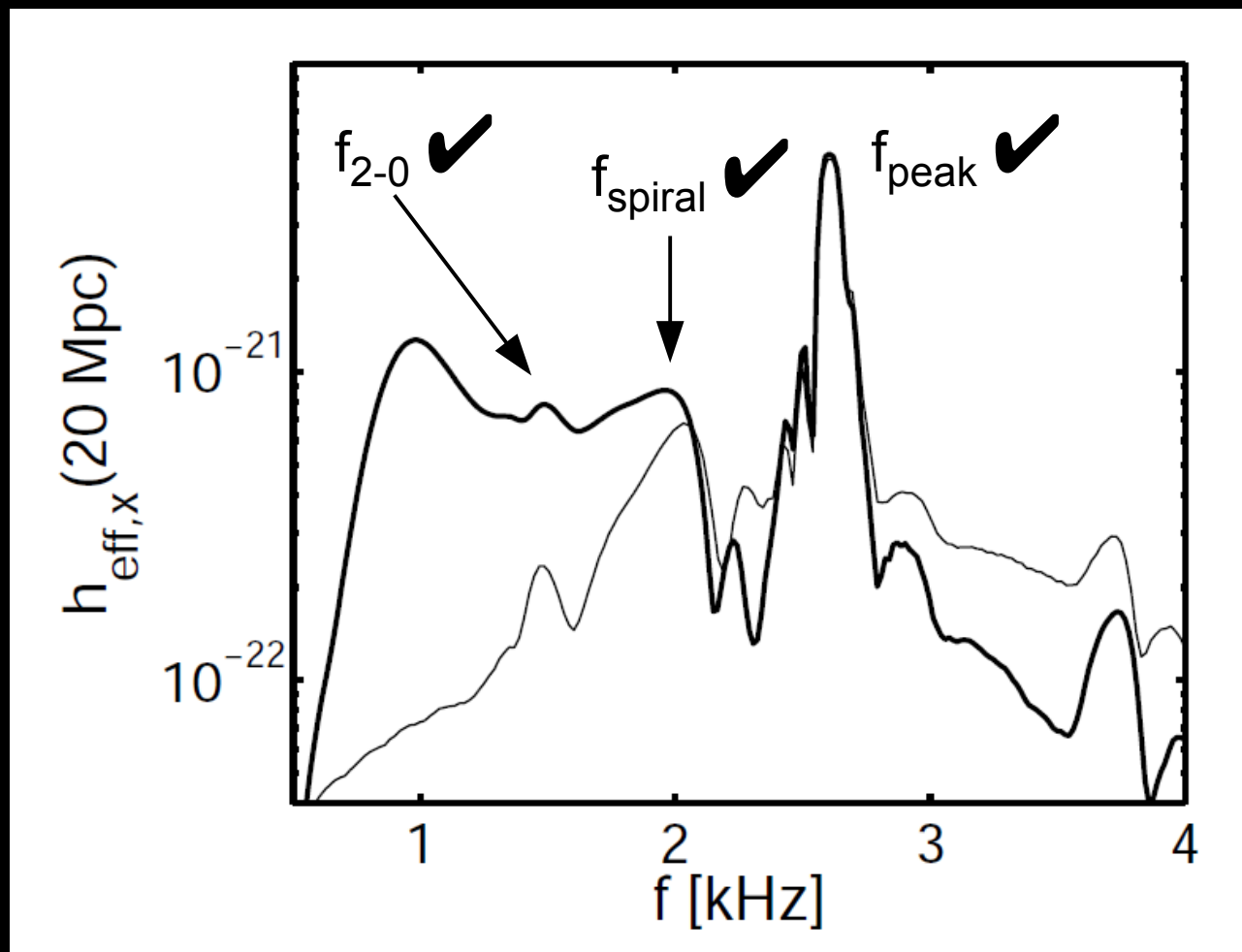
Orbital motion of **antipodal bulges** slower than inner part of the remnant (**double-core structure**)

Spiral pattern, created during merging lacks behind

Orbital frequency:
1/1ms → generates GW at 2 kHz !!!

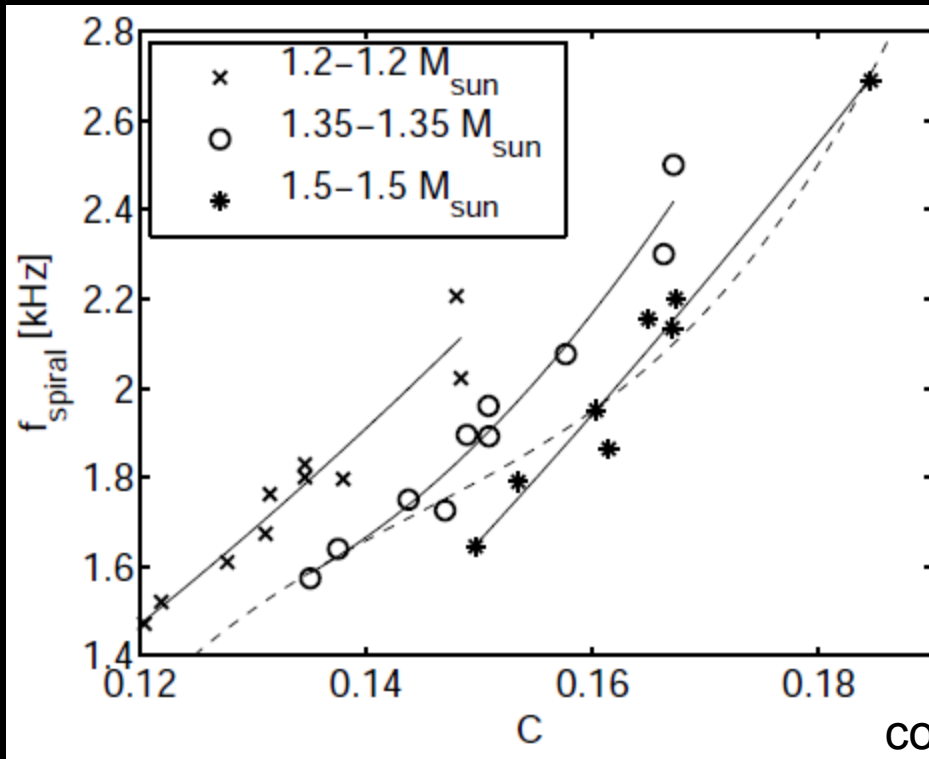
Present for only a few ms / cycles

Generic GW spectrum

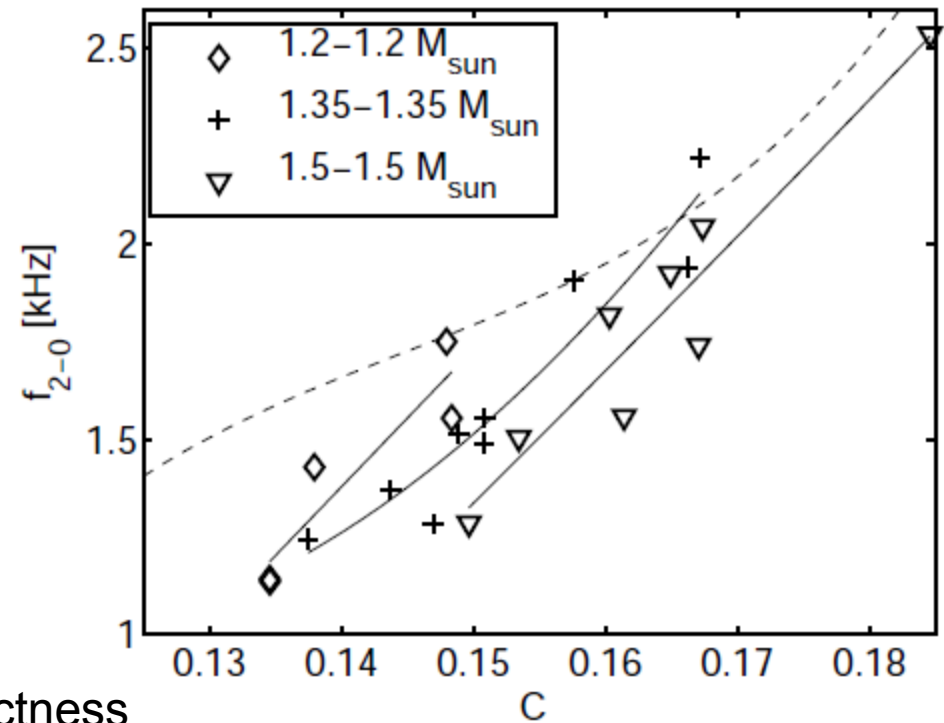


- Orbital motion of antipodal bulges generate peak at f_{spiral}

Different binary masses



Bauswein et al. 2015



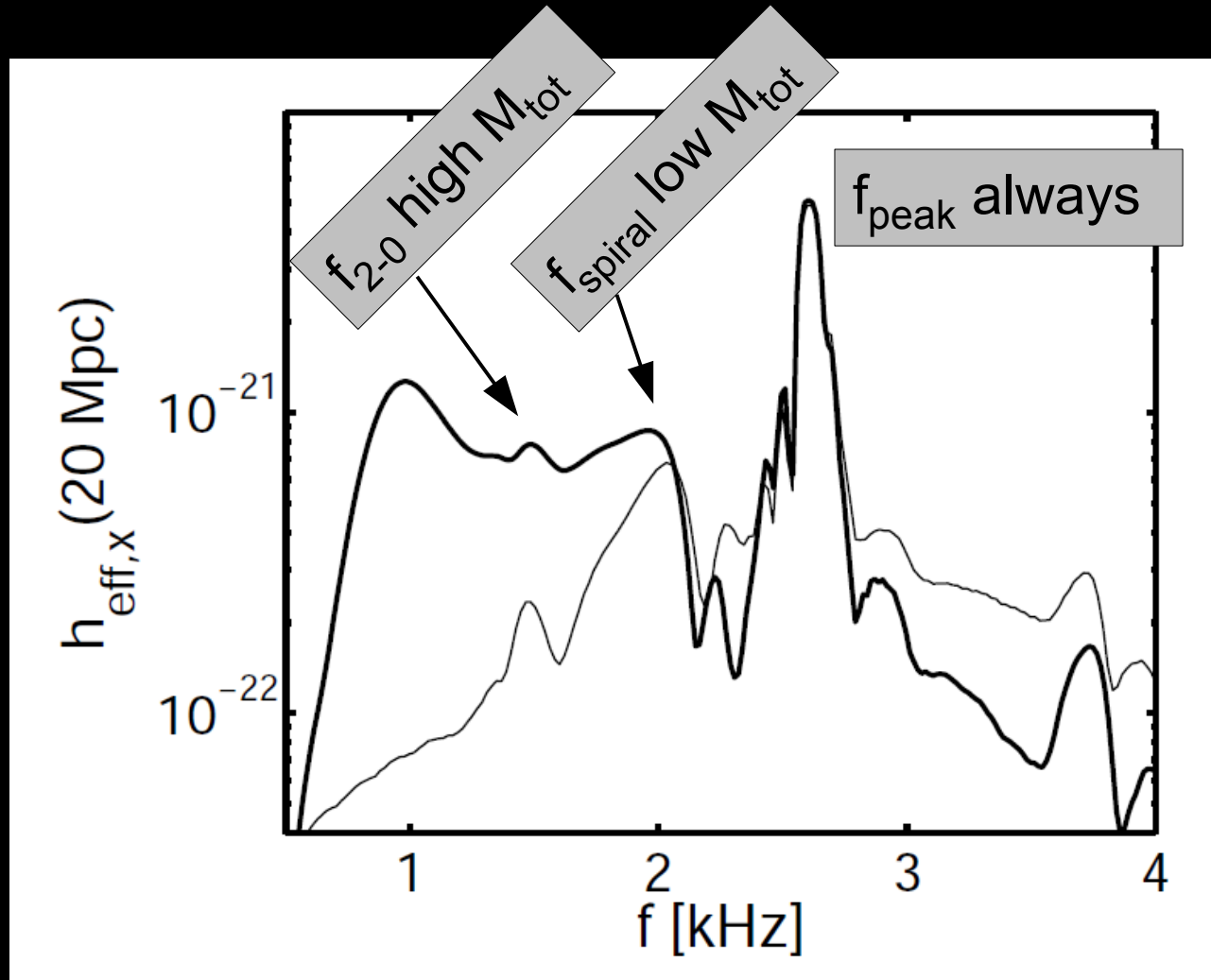
Dashed line from Takami et al. 2014

- ▶ for the individual secondary frequencies there are **relations** between C and the frequency **for fixed binary masses** (solid lines)
- ▶ (binary masses will be known from GW inspiral signal)
- ▶ mass-dependent relations for secondary peaks – not all equally strong!

Secondary peaks

- ▶ Strength of secondary peaks leads to **classification scheme of postmerger spectra and dynamics** → 3 types of spectra
- ▶ Origin and dependencies of secondary peaks still under debate
- ▶ More features to be identified
- ▶ Detection of secondary features challenging

Survey of GW spectra



- Considering different models (EoS, M_{tot}): **3 types of spectra depending on presence of secondary features (dominant f_{peak} is always present)**

Summary

- ▶ NS mergers are multi-messenger events: r-process nucleosynthesis, kilonovae, short gamma-ray bursts, gravitational waves → highly rewarding
- ▶ GWs from NS mergers expected any time
- ▶ EoS impact on inspiral
- ▶ Dominant postmerger oscillation frequency scales with NS radius → accurate and robust measurements
- ▶ GW data analysis ready for the postmerger (still improving)
- ▶ Collapse behavior of merger remnant → maximum mass of NSs (+ further properties)
- ▶ Secondary peaks towards GW asteroseismology → more details of the EoS