

An Adaptive Acceleration Structure for Screen-space Ray Tracing

Supplemental Material

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1 Pseudo code

Algorithm 1: GLSL pseudo-code for generating the bottom level of our traversal acceleration structure. λ_h and λ_d are set to 10^{-3} in our implementation.

```

input : depth;                                /* depth buffer data */
output: out;                                 /* node texture at level 0 */

1  $D_{0,0\dots2,2} \leftarrow \text{depth}$ ;           /* read 3x3 depth neighborhood */
2 /* discontinuity hint computed via Laplacian thresholding */
3  $O \leftarrow \text{step}(\lambda_d, \text{getLaplacian}(D))$ 
4 /* compute forward and backward differentials */
5  $df_{xy} \leftarrow \text{vec2}(D_{2,1} - D_{1,1}, D_{1,2} - D_{1,1})$ 
6  $db_{xy} \leftarrow \text{vec2}(D_{1,1} - D_{0,1}, D_{1,1} - D_{1,0})$ 
7 /* enforce smoothness by picking the smallest derivative */
8  $d_{xy} \leftarrow \text{mix}(df_{xy}, db_{xy}, \text{abs}(df_{xy}) < \text{abs}(db_{xy}))$ 
9 /* zero large derivatives that connect different surfaces */
10  $d_{xy} \leftarrow \text{step}(\lambda_h, \text{abs}(d_{xy})) \cdot d_{xy}$ 
11 /* compute normal */
12  $\vec{N} \leftarrow \text{normalize}(\text{cross}(\text{vec3}(P_{\text{size}}.x, 0, d_x), \text{vec3}(0, P_{\text{size}}.y, d_y)))$ 
13 /* compute plane's top-left corner z-coordinate */
14  $P \leftarrow D_{1,1} - \text{dot}(\vec{N}_{xy}/\vec{N}_z, -0.5 \cdot P_{\text{size}})$ 
15 out  $\leftarrow \text{outputPlane}(\vec{N}, P, O)$ ;          /* output a plane node */

```

We compare in Fig. 1 the depth reconstruction quality of our method against a gold-standard GPU ray tracer—NVIDIA OptiX [Parker et al. 2010]. Even though we only use two depth layers in this example, our approach correctly evaluates the depth at all pixels (except where three layers would be required), while being $3\times$ faster than general-purpose ray tracer. Note that our approach allows us to inpaint the remaining holes, so that no artifacts appear. Alternatively, one can simply use more layers.

References

- PARKER, S. G., BIGLER, J., DIETRICH, A., FRIEDRICH, H., HOBEROCK, J., LUEBKE, D., McALLISTER, D., MCGUIRE, M., MORLEY, K., ROBISON, A., AND STICH, M. 2010. OptiX: A general purpose ray tracing engine. *ACM Trans. Graph.* 29, 4.

Algorithm 2: GLSL pseudo-code for construction and compression of a single level of the quad-tree.

```

input : in;                                     /* node texture at level i ( $i > 0$ ) */
output: out;                                  /* node texture at level i-1 */
1  $Q_{0\dots3} \leftarrow \text{in};$                       /* read 2x2 neighboring nodes */
2 if containOnlyPlanes ( $Q_{0\dots3}$ ) then
3   /* get plane normal vector, origin and "discontinuity" flag */
4   ( $\vec{N}, P, O)_{0\dots3} \leftarrow \text{getPlaneData}(Q_{0\dots3})$ 
5   /* set proxy plane normal to mean of children normals */
6    $\vec{N}_{proxy} \leftarrow \text{normalize}(\text{mean}(\vec{N}_{0\dots3}))$ 
7   /* compute angle differences via dot-product */
8   float  $d_{0\dots3} \leftarrow 1 - \text{dot}(\vec{N}_{proxy}, \vec{N}_{0\dots3})$ 
9   /* proxy plane origin  $P_{proxy}$  is least-square fit to child planes with fit errors
    stored in  $p_{0\dots3}$  */
10  ( $P_{proxy}, p_{0\dots3}) \leftarrow \text{getPlaneOrigin}(\vec{N}_{proxy}, \vec{N}_{0\dots3}, P_{0\dots3})$ 
11  /* output a plane node if the proxy is close enough to children in terms of
    orientation and position */
12  if  $\max(d_{0\dots3}) < \gamma_{norm}$  and  $\max(p_{0\dots3}) < \gamma_{dist}$  then
13    out  $\leftarrow \text{outputPlane}(\vec{N}_{proxy}, P_{proxy}, \text{any}(O_{0\dots3}))$ 
14    return
15  end
16 end
17 /* output AABB node that encompasses all children */
18  $\text{vec2 } Z_{0\dots3} \leftarrow \text{getMinMaxZ}(Q_{0\dots3})$ 
19 float  $\min_z \leftarrow \min(Z_{0\dots3.x})$ 
20 float  $\max_z \leftarrow \max(Z_{0\dots3.y})$ 
21 out  $\leftarrow \text{outputAABB}(\min_z, \max_z)$ 

```

Algorithm 3: GLSL pseudo-code for ray traversal through a single depth layer. For brevity, we assume the quad-tree MIPMAP has power-of-two size.

```

input :  $T_0 \dots n-1$ ; /* texture MIPMAP storing depth quad-tree */
input :  $R$ ; /* ray structure storing direction and origin */
output: bool rayHit; /* trace result */
output: bool occlusionHit; /* did we hit an occlusion volume? */
output: float d; /* hit-point distance along the ray */
output: vec4 plane; /* hit-plane data */

1 int  $Q_{level} \leftarrow n - 1$ ; /* current quad-tree level, start at the root */
2 /* current node position in the quad-tree */ /* current node position in the quad-tree */
3 ivec2  $Q_{xy} \leftarrow \lfloor R.origin.xy * sizeof(T_0) / 2^{Q_{level}} \rfloor$ 

4 while insideBounds( $pos, T_{Q_{level}}$ ) do
5   vec2  $Q_{data} \leftarrow T_{Q_{level}}(Q_{xy})$ ; /* read the node data */
6   if nodeStoresPlane( $Q_{data}$ ) then
7     plane  $\leftarrow$  getPlaneData( $Q_{data}$ )
8     /* Get far and near Z of node
9     FandN  $\leftarrow$  getFarNearOfNode( $R, Q_{xy}, Q_{level}$ )
10     $\vec{N} \leftarrow plane.xyz$ ; /* plane normal */
11     $P_0 \leftarrow vec3(Q_{xy}/2^{Q_{level}}, plane.w)$ ; /* and origin */
12    /* compute ray-plane intersection */ /* compute ray-plane intersection */
13     $d \leftarrow dot(P_0 - R.origin, \vec{N}) / dot(R.dir, \vec{N})$ 
14    if dot( $R.dir, \vec{N}$ )  $> 0$  then /* plane is front-facing the ray */ /* if dot(R.dir, N) > 0 then /* plane is front-facing the ray */
15      if  $d < FandN.near$  then occlusionHit  $\leftarrow$  true;
16      if  $d \geq FandN.near$  and  $d < FandN.far$  then
17        rayHit  $\leftarrow$  true
18        plane  $\leftarrow$  vec4( $\vec{N}, dot(P_0, \vec{N})$ )
19        return
20      end
21    else /* plane is back-facing the ray */ /* else /* plane is back-facing the ray */
22      if  $d \geq FandN.near$  then occlusionHit  $\leftarrow$  true;
23    end
24  else
25    /* compute intersection with both node bounding box and occlusion
       volume */ /* compute intersection with both node bounding box and occlusion
       volume */
26    ( $hitAABB, hitOV$ )  $\leftarrow$  rayIntersectAABB( $R, Q_{data}$ ) /* (hitAABB, hitOV) ← rayIntersectAABB(R, Qdata) */
27    if hitAABB then
28      if hitAABB.near  $=$  hitOV.far then
29        occlusionHit  $\leftarrow$  true
30      end
31      /* progress down to the next child */ /* progress down to the next child */
32      ip  $\leftarrow R.dir.xy * hitAABB.near + R.origin.xy$ 
33       $Q_{xy} \leftarrow Q_{xy} * 2 + step(0, ip - (Q_{xy} + 0.5)/2^{Q_{level}})$ 
34       $Q_{level} \leftarrow Q_{level} - 1$ 
35      continue
36    else
37      if hitOV then occlusionHit  $\leftarrow$  true;
38    end
39  end
40  /* plane or AABB miss, progress to the next node */ /* plane or AABB miss, progress to the next node */
41  /* current node successor position at  $Q_{level}$  */ /* current node successor position at Qlevel */
42   $Q_{xy}^* \leftarrow getNextNode(R, Q_{xy}, Q_{level})$  /* compute how many levels up we need to go */
43  int levelShift  $\leftarrow$  findMSB( $((Q_x \oplus Q_x^*) \mid (Q_y \oplus Q_y^*))$  /* prevent the traversal from going above the quad-tree root */
44   $Q_{level}^* \leftarrow \min(Q_{level} + levelShift, n - 1)$  /* update the node location and level to new values */
45   $Q_{xy} \leftarrow \lfloor Q_{xy}^*/2^{(Q_{level}^*-Q_{level})} \rfloor$ 
46   $Q_{level} \leftarrow Q_{level}^*$ 
47 end
48 rayHit  $\leftarrow$  false

```

Algorithm 4: GLSL pseudo-code for finding coordinates of the next node that intersects with the ray in screen-space.

```

Function getNextNode( $Ray R, ivec2 Q_{xy}, int Q_{level}$ ) /* get node exit corner coordinate */
1  $vec2 B \leftarrow (Q_{xy} + step(0, R.dir.xy)) / 2^{Q_{level}}$  /* get distances to node edges that intersect at  $B_{xy}$  */
2  $vec2 D \leftarrow (B - R.origin.xy) / R.dir.xy$  /* compute position shift */
3  $ivec2 S_{xy} \leftarrow sign(R.dir.xy) * step(D.xy, D.yx)$  /* return new position */
4 return  $Q_{xy} + S_{xy}$ ;

```



Figure 1: A comparison of depth reconstruction quality. (a) A new view synthesized with our method (using two depth-layers). The full-image took 6.5ms to render. The synthesized depth for (b) two-layer and a (c) single-layer configuration. (d) The reference was generated with NVIDIA OptiX in about 20ms. In both cases we report combined construction and tracing times.